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Investigating the hydration of inner Earth minerals through *ab initio* random structure searching and solid-state NMR spectroscopy

David McKay

Robert Moran

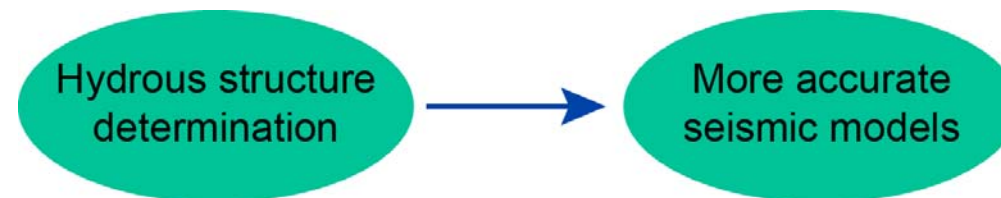
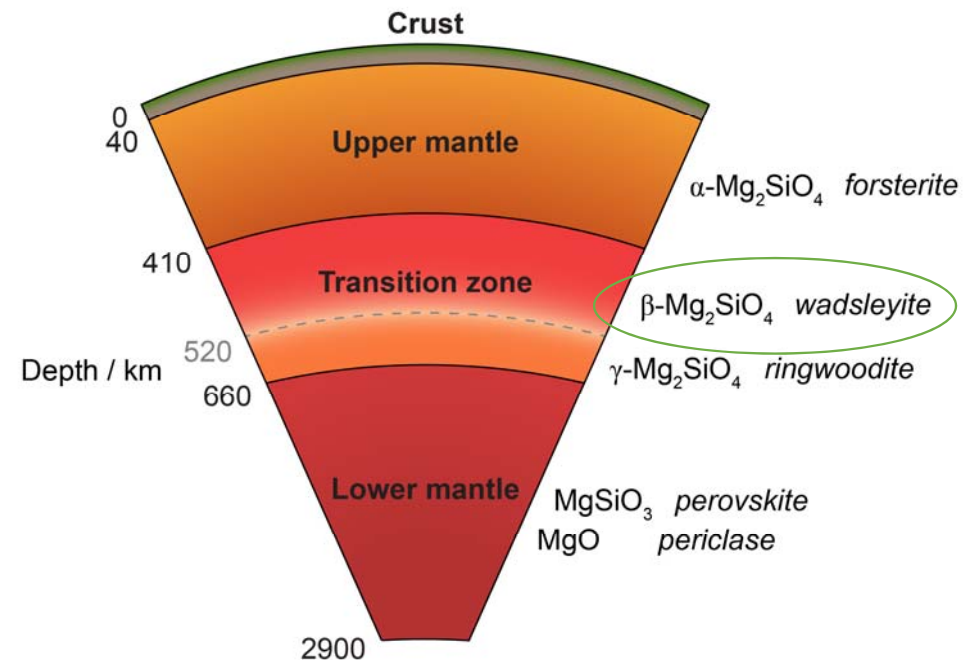
Daniel Twist

Sharon Ashbrook

Andrew Berry (ANU), Chris Pickard (Cambridge), Simone Sturniolo and Jonathan Yates (STFC, Oxford)

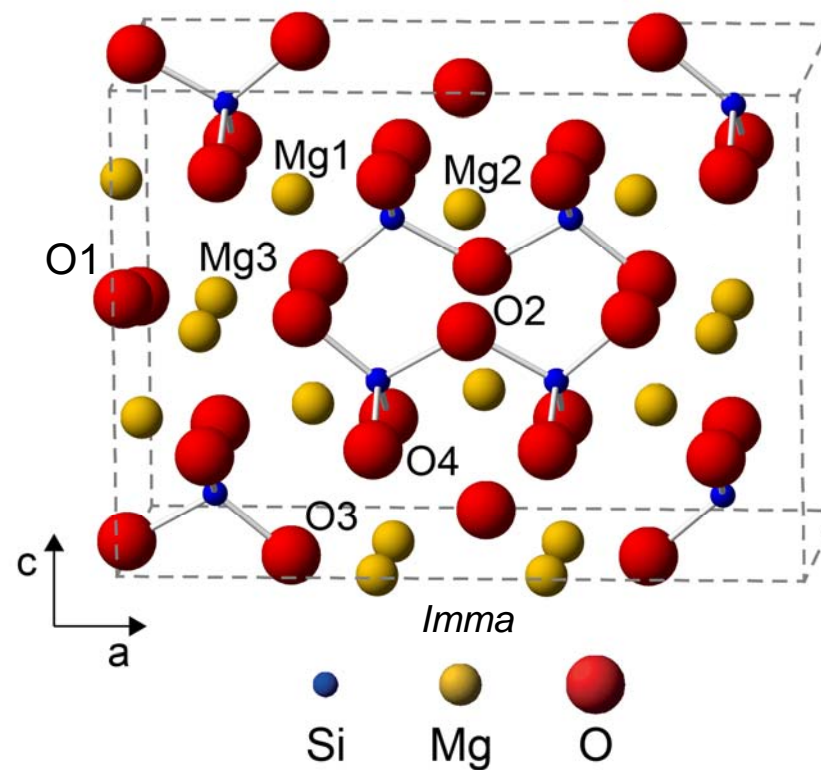
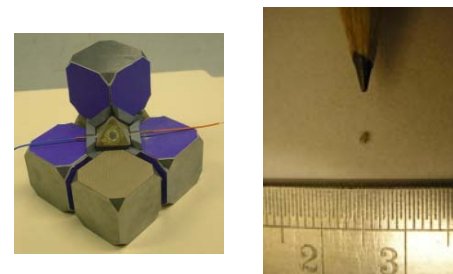
Inner Earth mineral hydration – Fe-free wadsleyite

- the Earth's mantle is composed mainly of magnesium silicates known as nominally anhydrous minerals (NAMs)
- phase transitions within the mantle
 - α - to β - Mg_2SiO_4 at ~410 km
 - γ - Mg_2SiO_4 to $\text{MgO}/\text{MgSiO}_3$ at ~660 km
 - β - to γ - Mg_2SiO_4 at ~520 km
- NAMs can be hydrated at mantle temperature and pressure – the location of the Earth's “missing water”
 - Mg_2SiO_4 1 – 3 wt% H_2O
 - MgSiO_3 0.01 – 0.1 wt% H_2O
- the structures of hydrous NAMs and the effects of hydration on the physical properties of the mantle are not fully understood



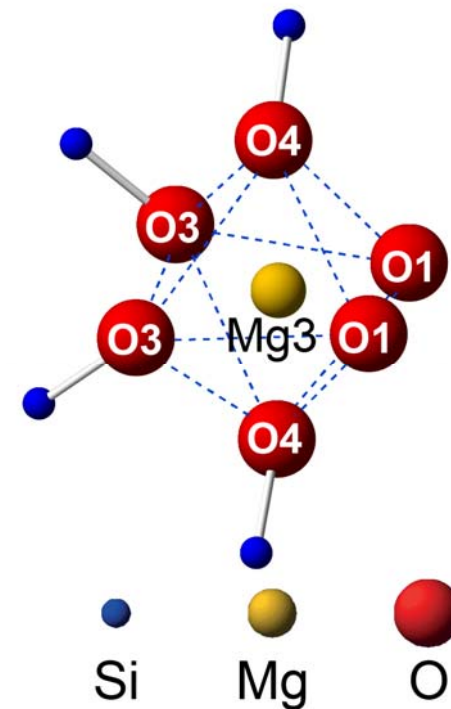
Wadsleyite

- 16 Mg^{2+} , $4 [\text{Si}_2\text{O}_7]^{6-}$ (pyrosilicate), 4 O^{2-}
- 3 Mg sites, 4 O sites, 1 Si site
- synthesis: 14-15 GPa, 1100-1200 °C, 1-20 mg
- suggested mechanism is loss of Mg^{2+} charge balanced by 2 H^+ giving net hydration
- $1 \text{ Mg}^{2+} / 2 \text{ H}^+ = \text{semi-hydrous (1.6 wt\% H}_2\text{O)}$
- $2 \text{ Mg}^{2+} / 4 \text{ H}^+ = \text{hydrous (3.3 wt\% H}_2\text{O)}$
- tentative literature consensus: Mg3 vacancies
- no consensus: location of hydrogen



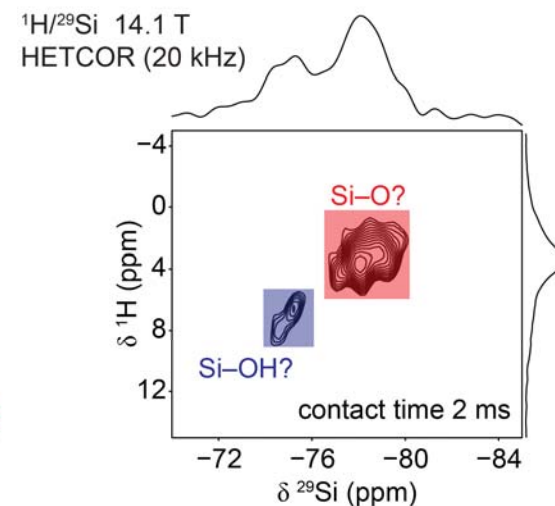
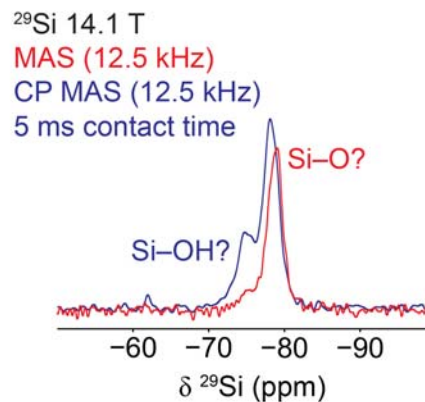
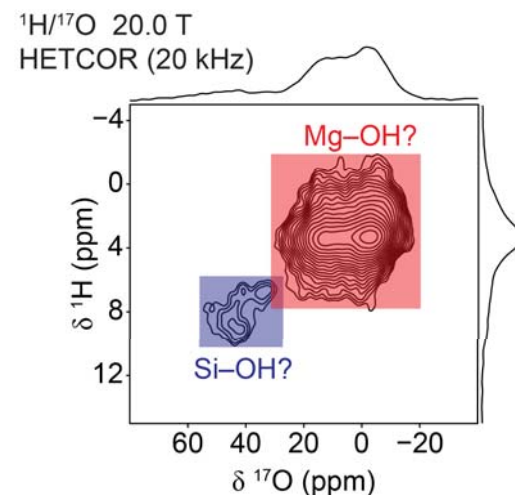
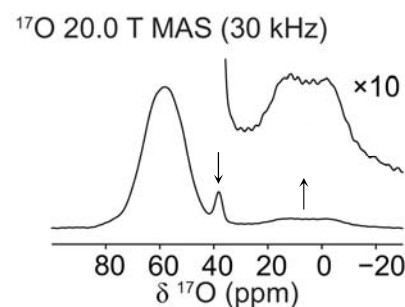
Hydrated wadsleyite – diffraction

- H location challenging for diffraction
- hydration introduces disordered cation vacancies
- from neutron diffraction (on deuterated sample):
 - Mg3 88 % occupancy (Mg1 99 %; Mg2 100 %)
 - H⁺ bound to O1, H-bonding to O4 (O1–H...O4)
 - “We were unable to find evidence of protonation of O2, O3, and O4... Further study is necessary to investigate whether there are the other sites of hydrogen or not.”
- diffraction suggests silanol OH groups *are not* present



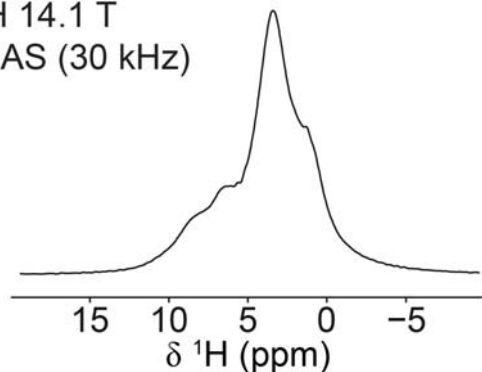
Hydrated wadsleyite – solid-state NMR spectroscopy (~3.3 wt% H₂O)

- not reliant on long-range order
- gives site- and element-specific information
- ¹⁷O NMR
 - confirms hydration
 - two distinguishable ¹⁷O–¹H environments
- ²⁹Si NMR
 - two types of ²⁹Si environment – one in close proximity to ¹H
- NMR suggests silanols are present



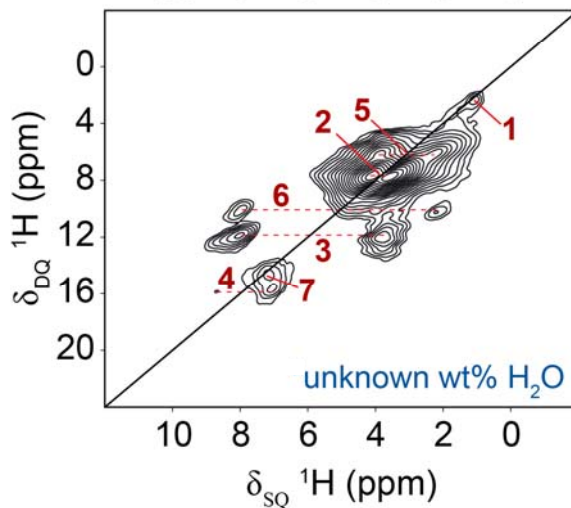
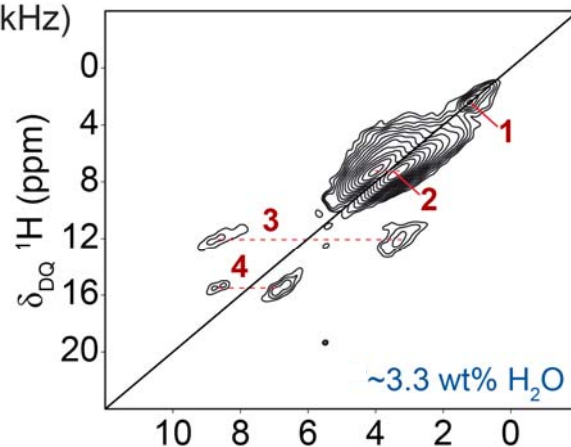
Hydrated wadsleyite – solid-state NMR spectroscopy (~3.3 wt% H₂O)

¹H 14.1 T
MAS (30 kHz)



¹H 1-D spectrum shows 4-6 peaks

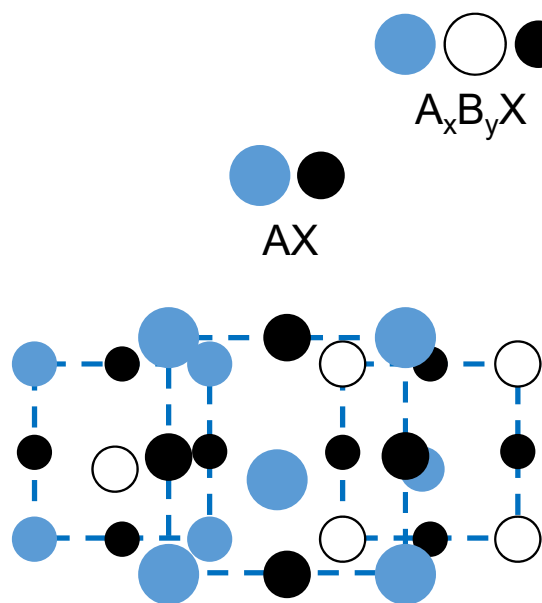
¹H 14.1 T
DQ MAS (30 kHz)



Correlation	δ ¹ Ha (ppm)	δ ¹ Hb (ppm)
1	1.1	1.1
2	3.4	3.4
3	3.4	8.6
4	6.7	8.6
5	2.0	3.4
6	2.0	8.6
7	6.7	6.7

- ¹H at 1.1 ppm does not couple to different ¹H – potential impurity
- (almost) all other ¹H species correlate – more later

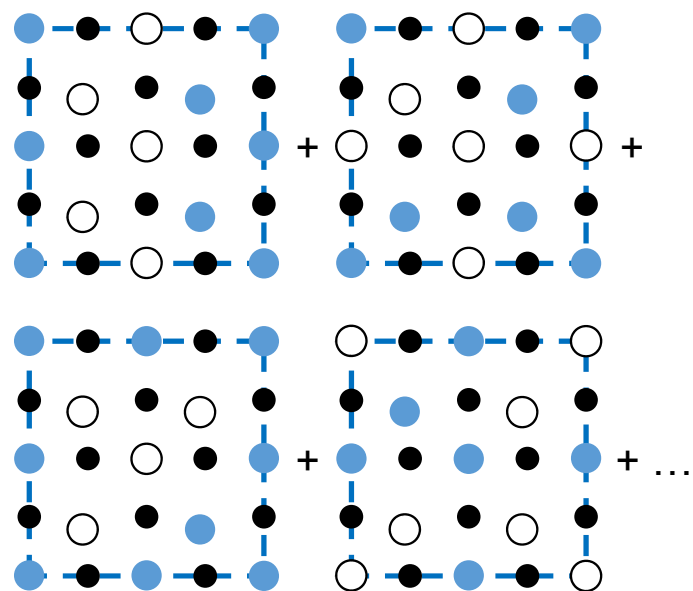
Modelling disorder



I

simple swapping of atoms
< 10 models
done manually

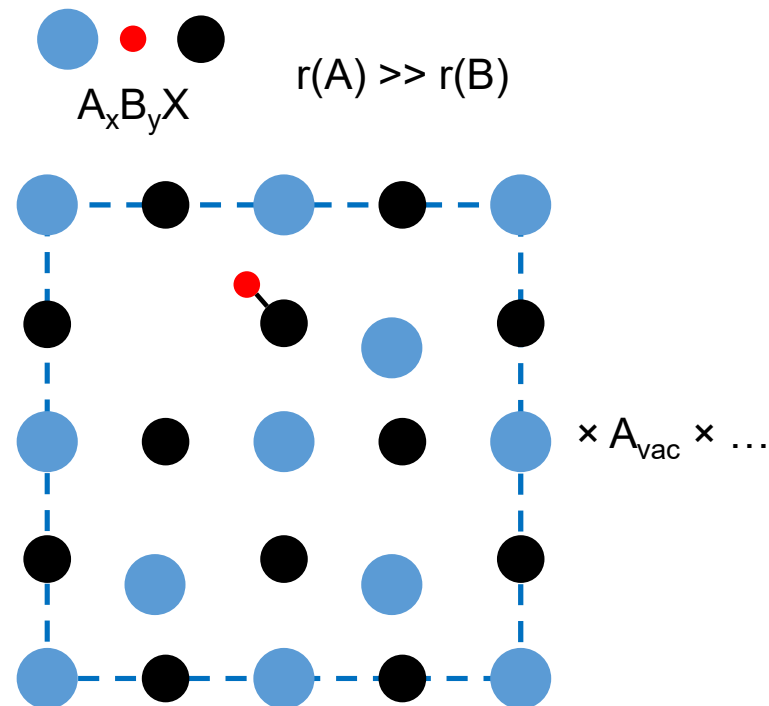
$r(A) \approx r(B)$



II

systematic swapping of atoms
10s to 100s of models
manually or automated
consider symmetry

$r(A) \gg r(B)$

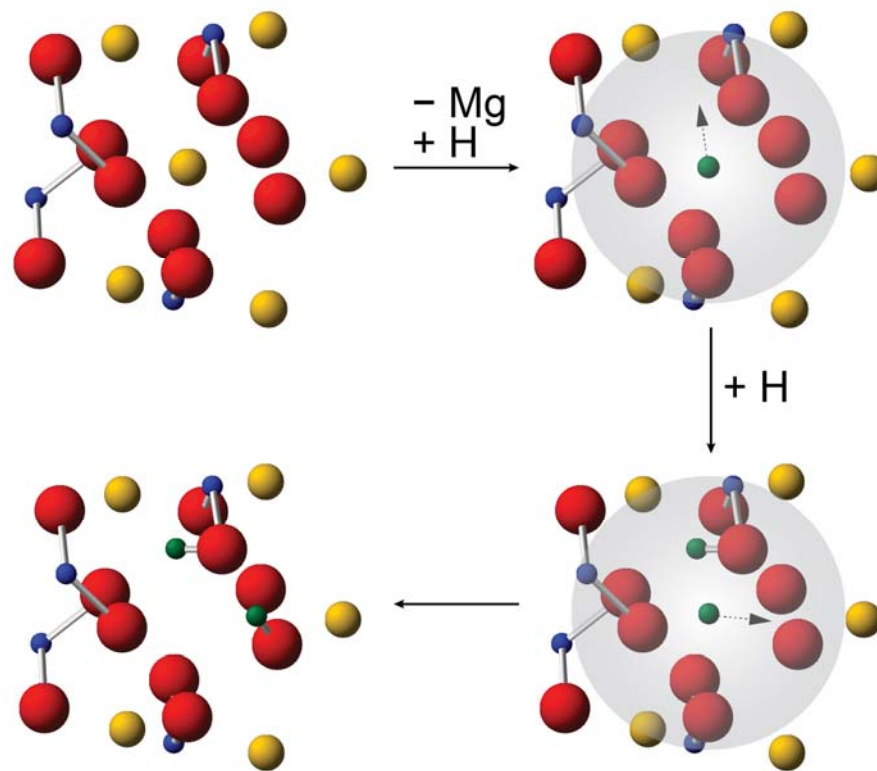


III

simple removal, complex addition
100s to 1000s of models
automated
potentially combinatorial

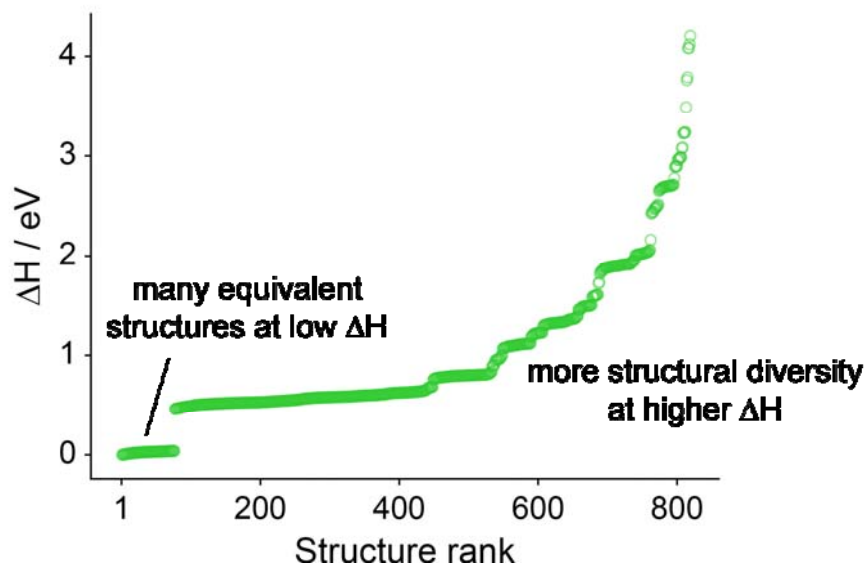
AIRSS approach to hydrous Mg_2SiO_4

- for each Mg removed, place 2 H
- but H^+ too small to occupy octahedral sites
- use *ab initio* Random Structure Searching (AIRSS) to randomise H positions within a 3 Å radius of Mg vacancy
- repeat ~100-1000 times
- geometry optimise in CASTEP
 - PBE
 - $E_{\text{cut}} = 25 \text{ Ry}$
 - k-point spacing = $0.1 \text{ } 2\pi/\text{\AA}$
 - fixed unit cell
 - ~1 structure per node hour



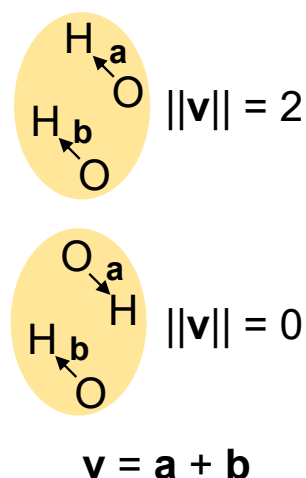
C. J. Pickard and R. J. Needs, *Phys. Rev. Lett.*, 2006, **97**, 045504.
C. J. Pickard and R. J. Needs, *J. Phys.: Condens. Matter*, 2011, **23**, 053201.
R. Moran, *et al.*, *Phys. Chem. Chem. Phys.*, 2016, **18**, 10173.

k-means clustering through Soprano



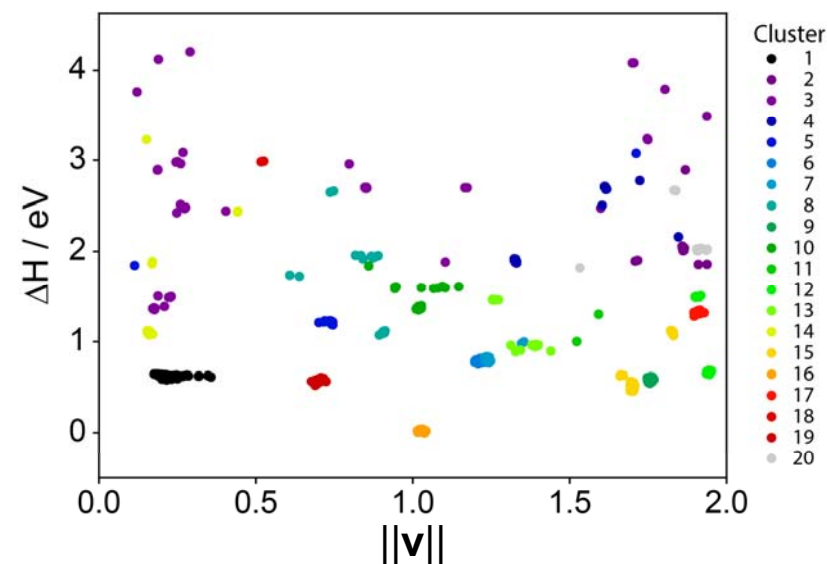
Clustering

- in-house Python scripts used the Soprano library
- “genes” were built for enthalpy, vac type, hydroxyl O type, combined OH orientation vector, vac...vac dist
- converge against number of clusters, k
- O type gene weighted such that each cluster contained structures with a single O type



Selection

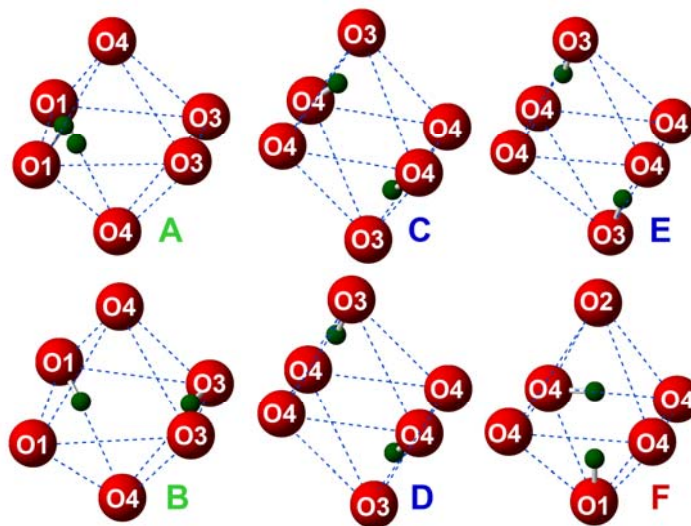
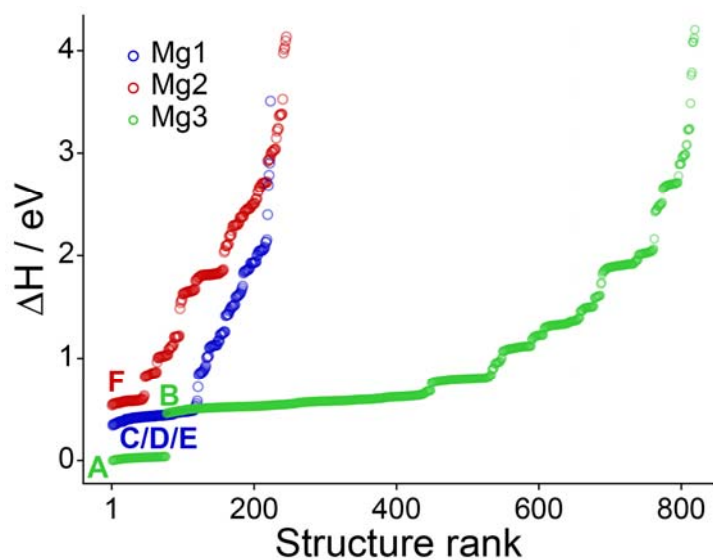
- only consider clusters with a mean $\Delta H < \Delta H_{\text{cut}}$ (here, 2 eV)
- always select the most stable structure
- for narrow clusters, select the median ΔH structure
- for broad clusters, include structures at the 5th and 95th percentiles



Semi-hydrated wadsleyite

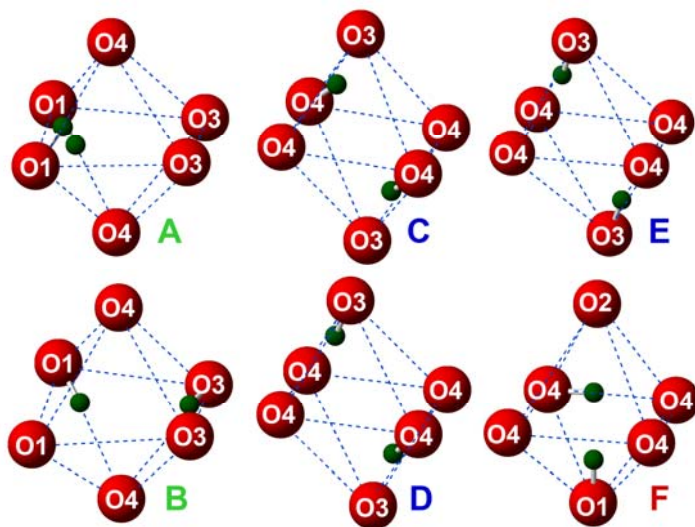
1287 structures with one Mg1, Mg2 or Mg3 vacancy

88 structures following k-means clustering

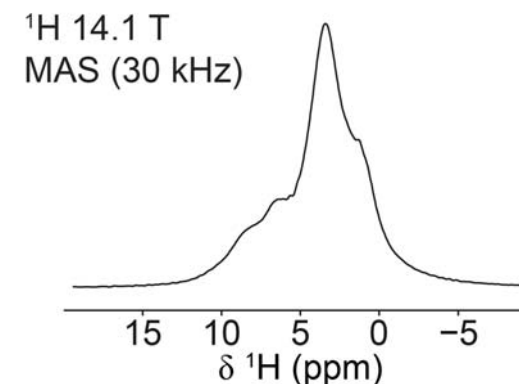


- subset of 88 structures “fully” optimised with PBE, $E_{\text{cut}} = 60 \text{ Ry}$, k-point spacing = $0.04 \text{ } 2\pi/\text{\AA}$, TS dispersion correction and variable unit cell
- GIPAW NMR calculations at the same level

Semi-hydrated wadsleyite



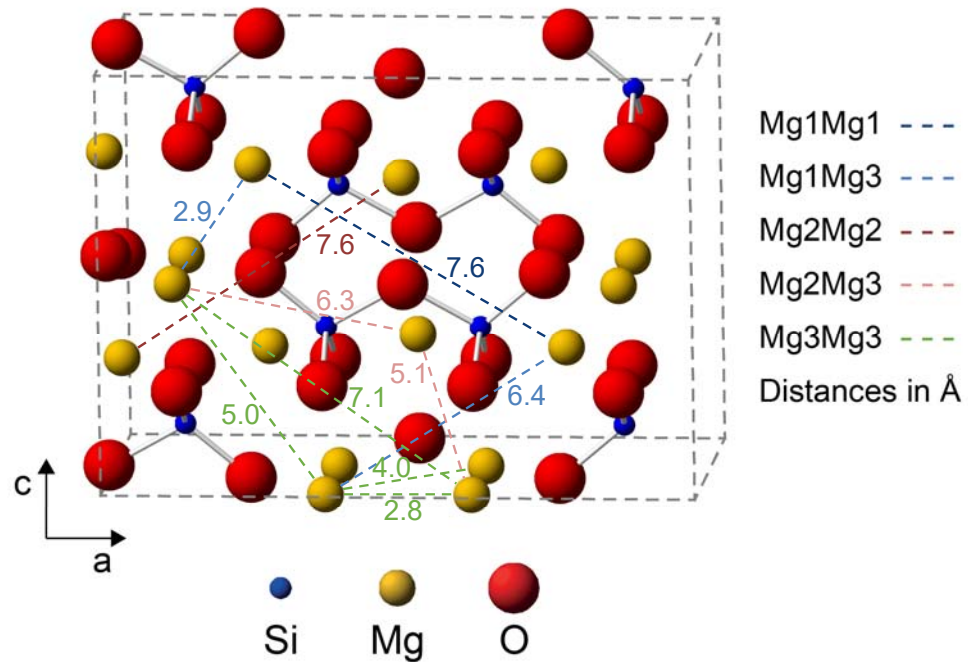
Structure	ΔH / eV	$^1\text{H } \delta_{\text{iso}}$ (ppm)	O type
A	0.00	3.4	1
		3.4	1
B	0.50	2.7	1
		6.4	3
C	0.33	8.5	4
		8.7	4
D	0.37	10.8	3
		8.9	4
E	0.37	10.0	3
		10.0	3
F	0.56	2.5	1
		7.7	4



Correlation	δ $^1\text{H}_a$ (ppm)	δ $^1\text{H}_b$ (ppm)
1	1.1	1.1
2	3.4	3.4
3	3.4	8.6
4	6.7	8.6
5	2.0	3.4
6	2.0	8.6
7	6.7	6.7

- shifts of O1– ^1H species in ground-state structure, A, align with the most intense experimental peak
- Include O1–H hydroxyls and O3–H and O4–H silanol groups, allowing tentative assignment of O1– ^1H , O3– ^1H and O4– ^1H to peaks at 3.4, 6.7 and 8.6 ppm respectively
- however:
 - require high ΔH proton arrangements and disfavoured Mg2 vacancies to explain the 1D spectrum
 - some O3– ^1H shifts outside of the range seen experimentally
 - features present in 2D spectra cannot be accounted for

Fully-hydrated wadsleyite



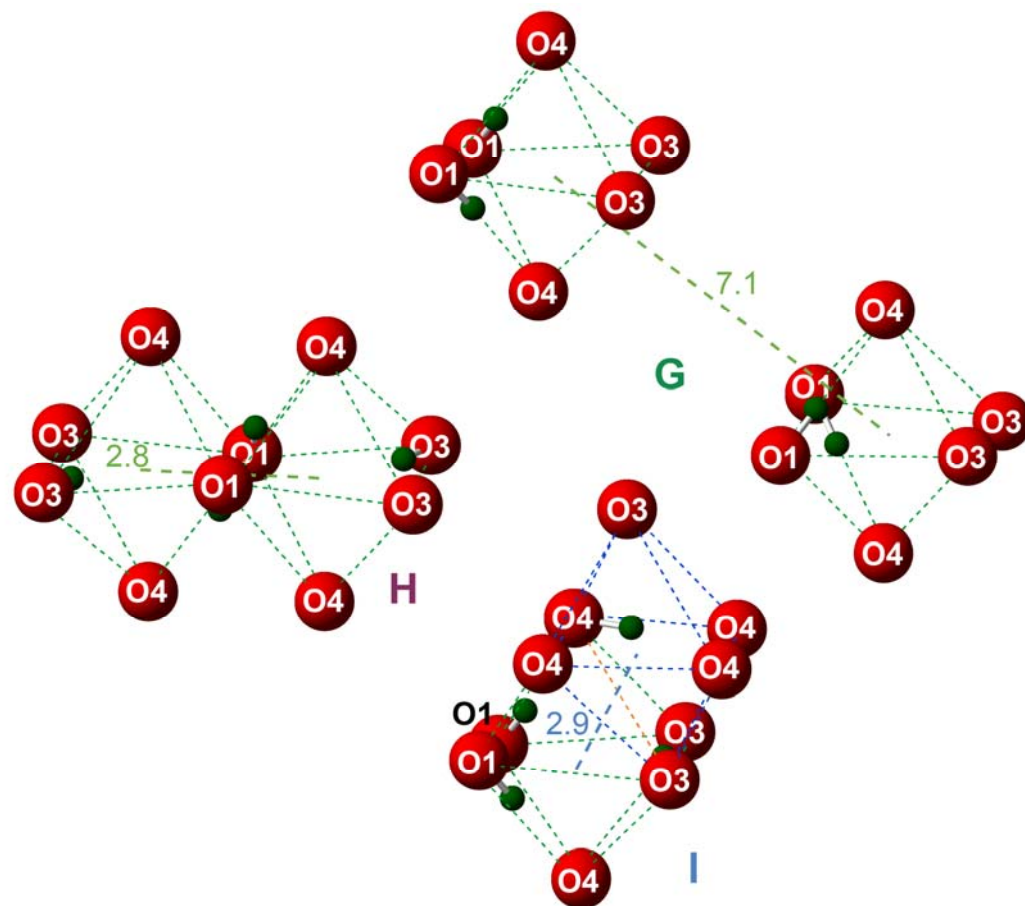
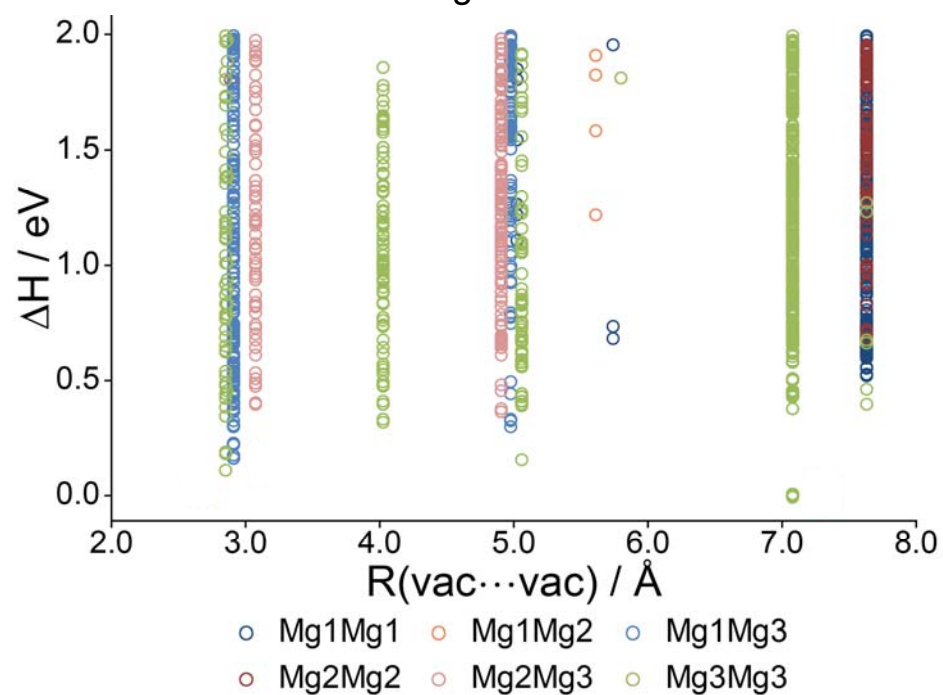
- to model full hydration need to remove two Mg atoms per unit cell
- vacancy combinations were chosen to give a range of vac...vac distances
- should provide information on the likelihood of defect clustering
- subject each vacancy combination to AIRSS-based addition proton of 4 H⁺

Fully-hydrated wadsleyite

3150 structures with combinations of two Mg vacancies

198 structures following k-means clustering

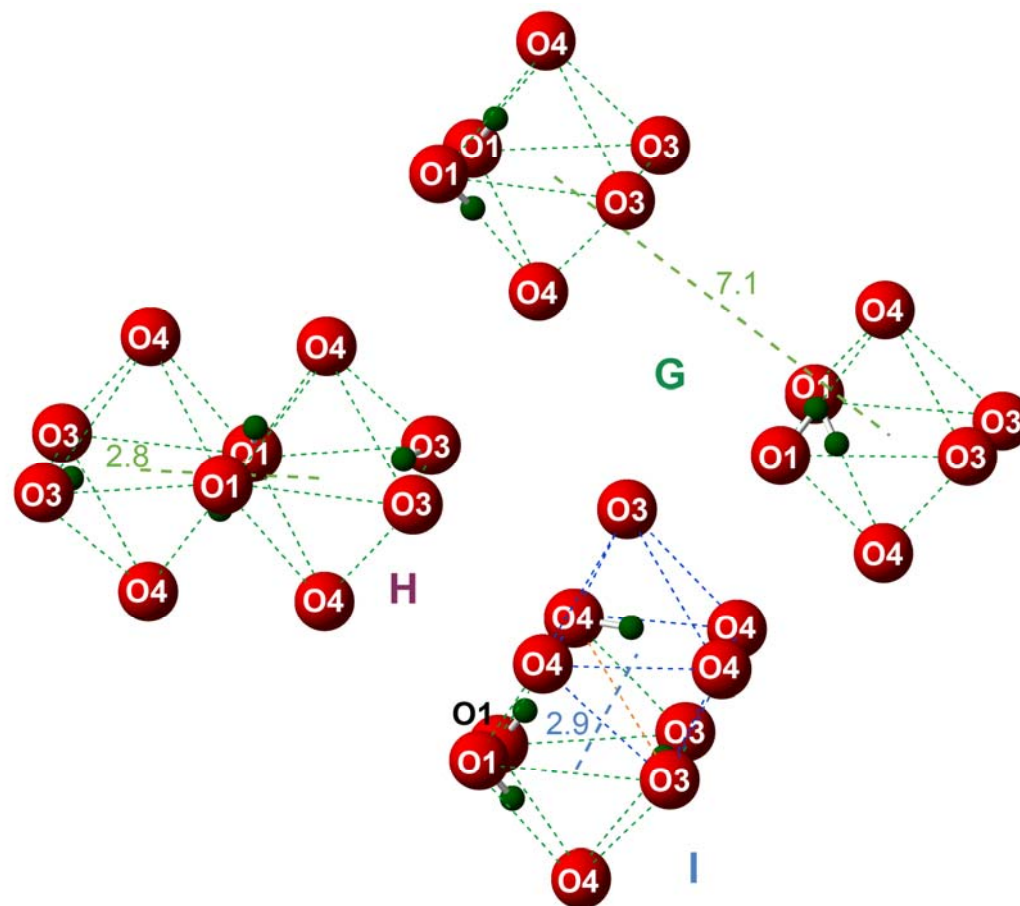
showing $\Delta H \leq 2.0$ eV



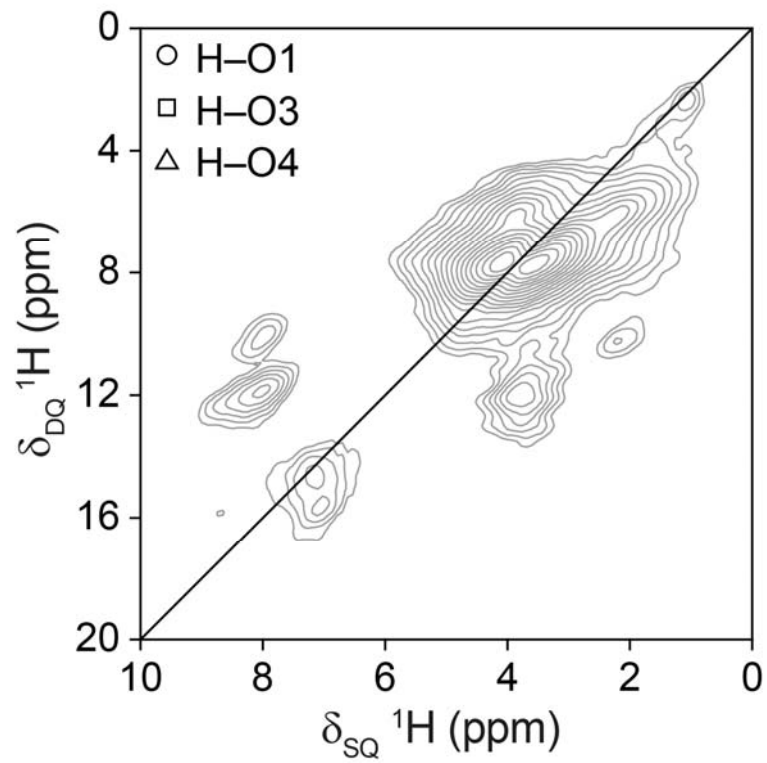
Fully-hydrated wadsleyite

Structure	ΔH / eV	vacs	vac...vac / Å ^a	¹ H δ_{iso} (ppm)	O type
G	0.00	Mg3 Mg3	7.1	3.3	1
				3.5	1
				3.5	1
				3.3	1
				1.9	1
H	0.22	Mg3 Mg3	2.8	6.8	3
				6.8	3
				1.9	1
				6.8	3
I	0.37	Mg1 Mg3	2.9	8.6	4
				2.2	1
				3.8	1
				3.8	1

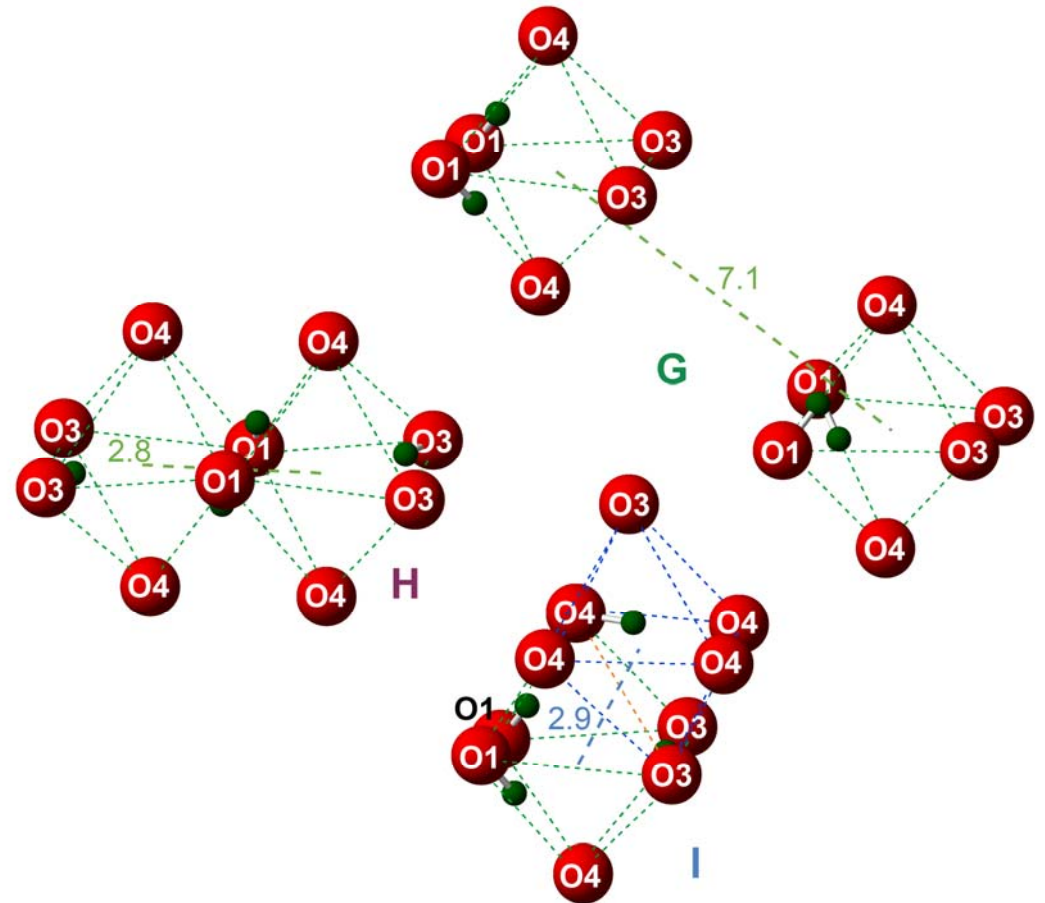
^a based on initial anhydrous wadsleyite



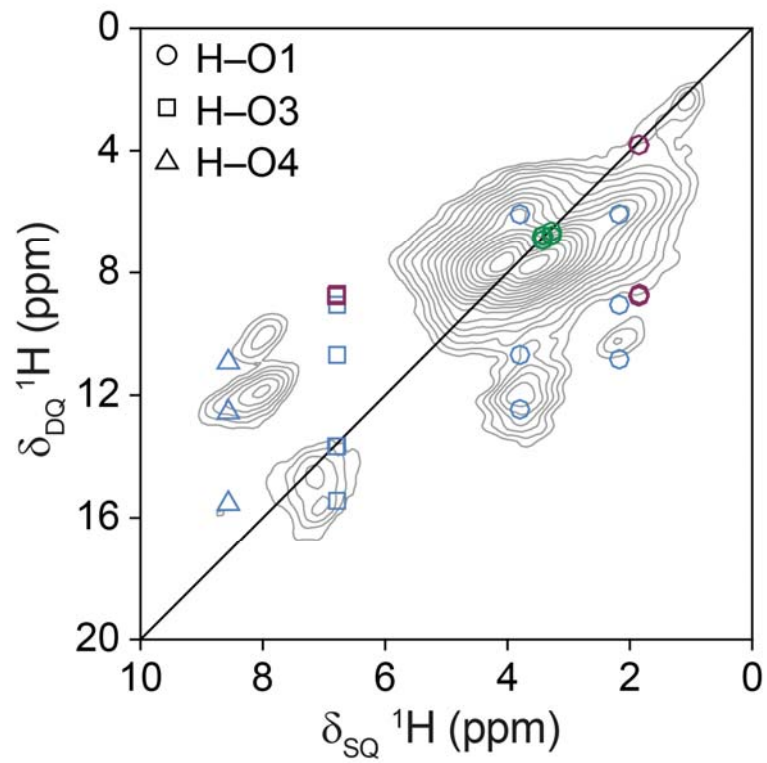
Fully-hydrated wadsleyite



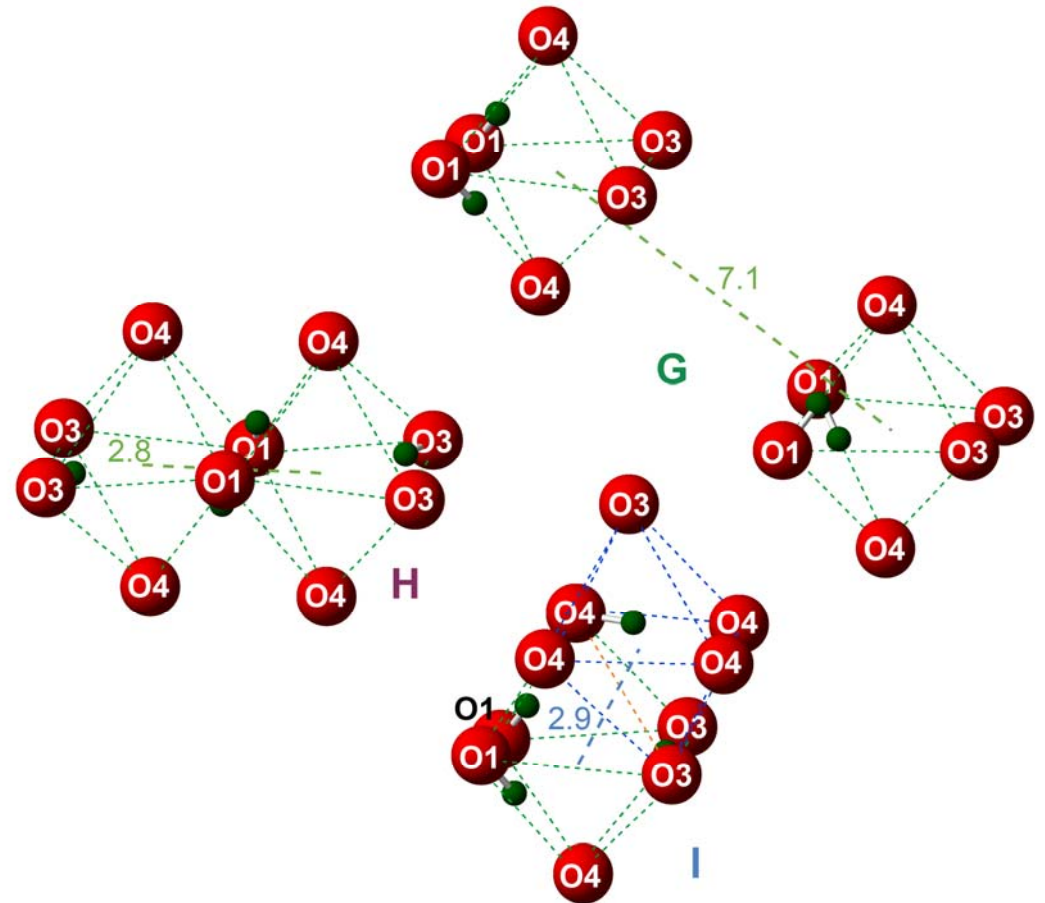
G
H
I



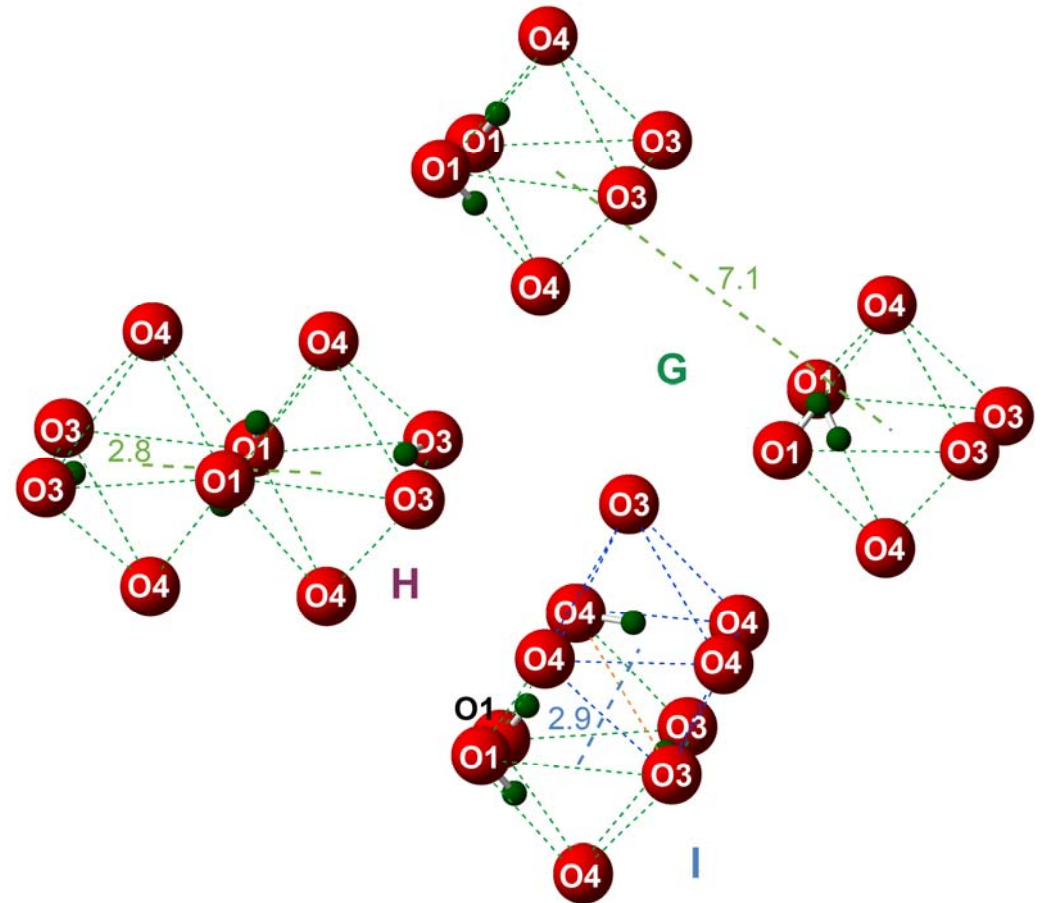
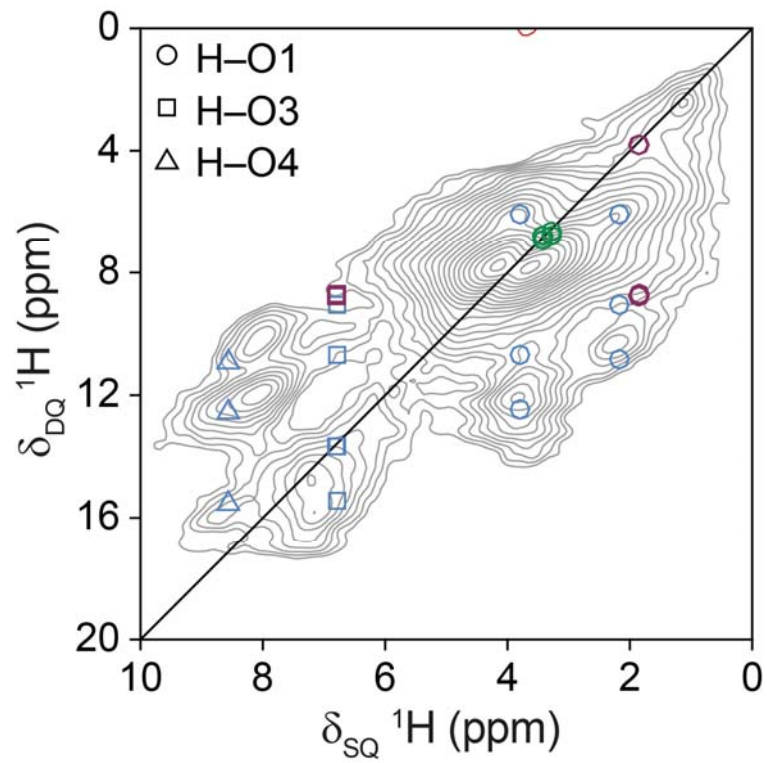
Fully-hydrated wadsleyite



G
H
I

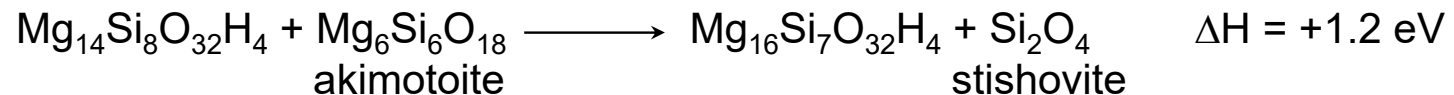


Fully-hydrated wadsleyite



Summary

- the ground-state structure of semi- or fully-hydrated wadsleyite results from Mg3 vacancies, charge balanced by protons, which bind to O1
- NMR experiments provide evidence of protonation of the pyrosilicate oxygens
- fully-hydrated structures allow full spectral assignment, showing O3 and O4 are protonated to form silanols
- calculations provide evidence for defect clustering
- O2 sites are not found to be protonated in any low enthalpy structure, its bridging position likely reducing its proton affinity
- alternative Si vacancies (not in the talk!) are discounted on enthalpy grounds (below) and due to excess Si used in synthesis to mimic the natural environment:





Prof. Sharon Ashbrook

Robert Moran

Daniel Twist

Ashbrook group

Collaborators:

Dr John Griffin

Dr Andrew Berry

Prof. Chris Pickard

Dr Simone Sturniolo

Dr Jonathan Yates

Computing facility:

Dr Herbert Früchtl