



Time-resolved photoionization: CS₂ and 1,3-cyclohexadiene

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The University of Edinburgh

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Glasgow

Photoionization: introduction



Aim:

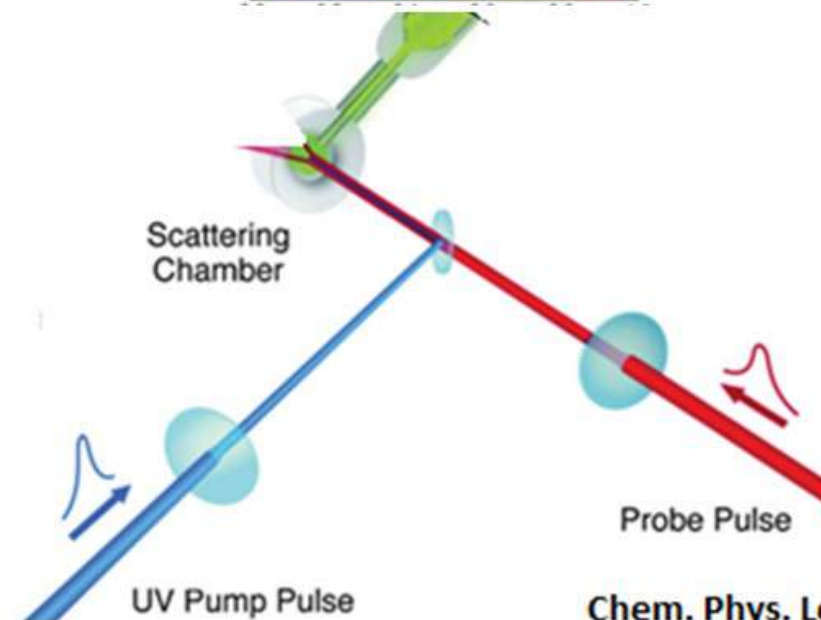
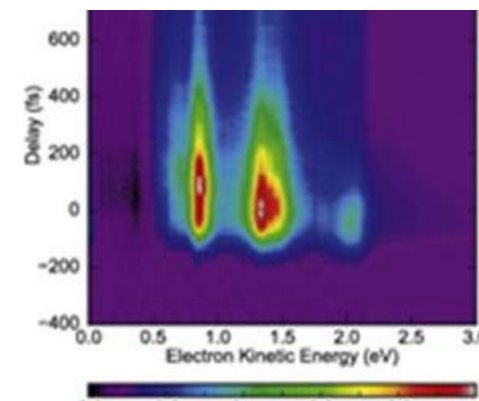
Pump-probe experiments in photochemistry



**Simulation tool for
time-dependent photoionization!**

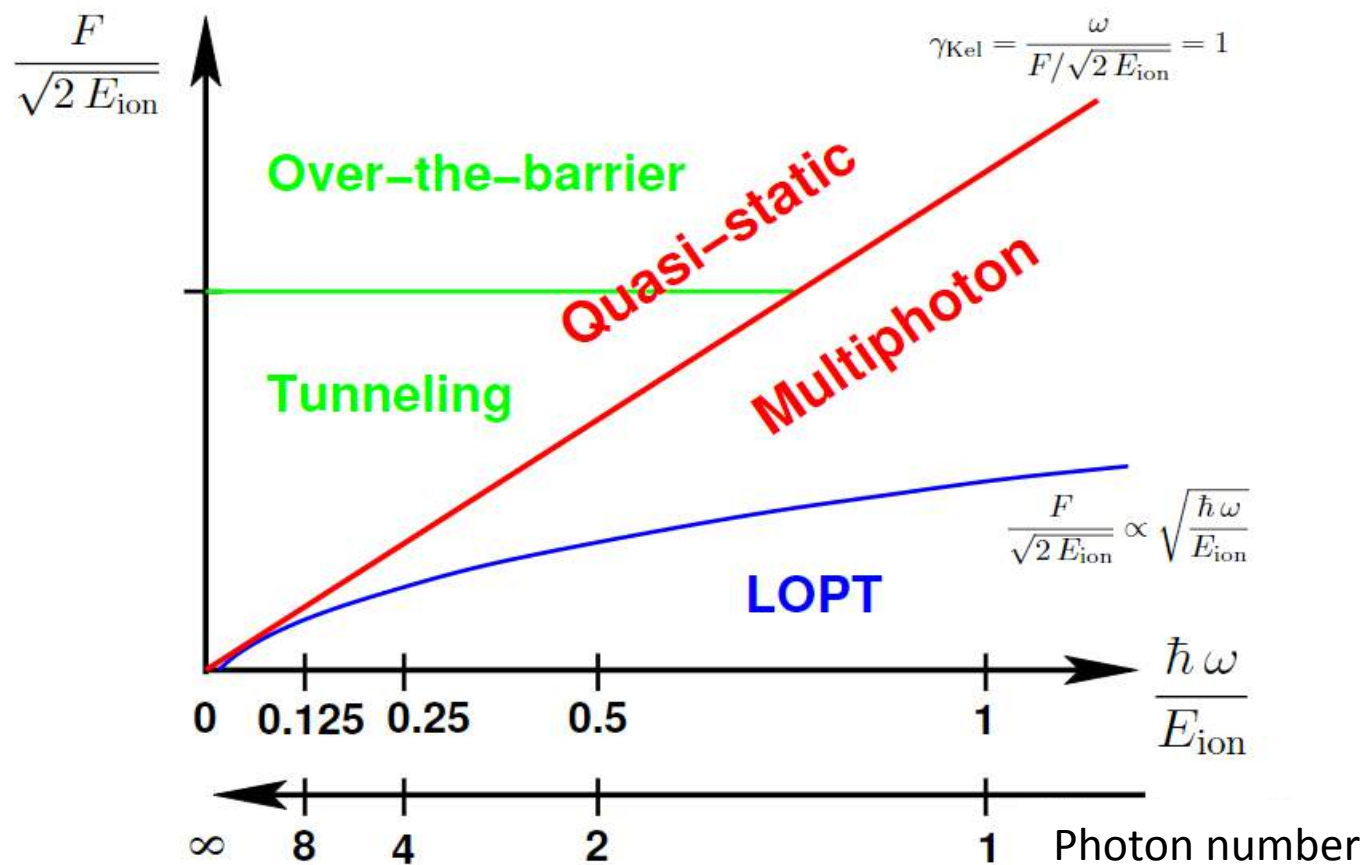
Outline:

- ✓ What is the photoionization rate?
- ✓ Methods
- ✓ CHD: channel-resolved photoionization
- ✓ CS₂: “average trajectory” approach
- ✓ Next steps



Chem. Phys. Lett.,
Bellshaw, D. *et al.*
2017

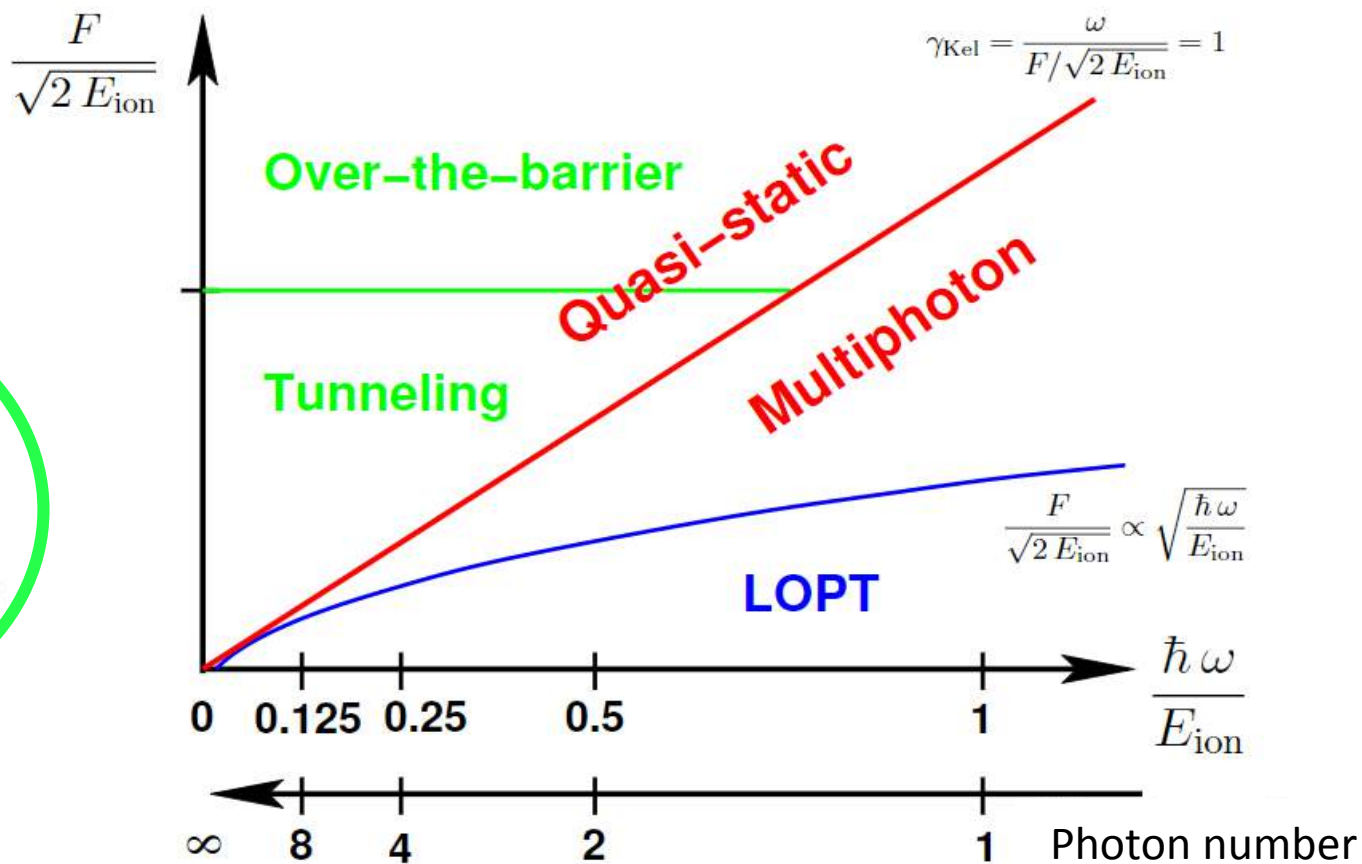
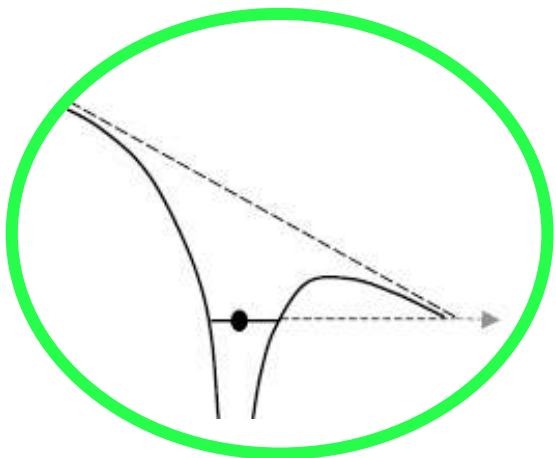
Photoionization regimes



A. Saenz: Atoms and Molecules in
B. Intense Laser Fields, Berlin 2014

F , ω (field strength & frequency); E_{ion} (ionization energy)

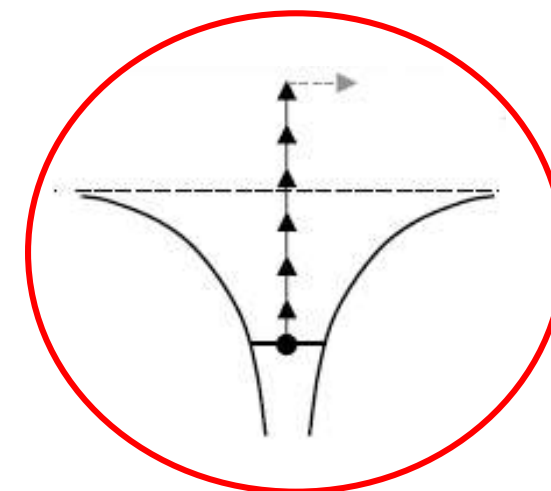
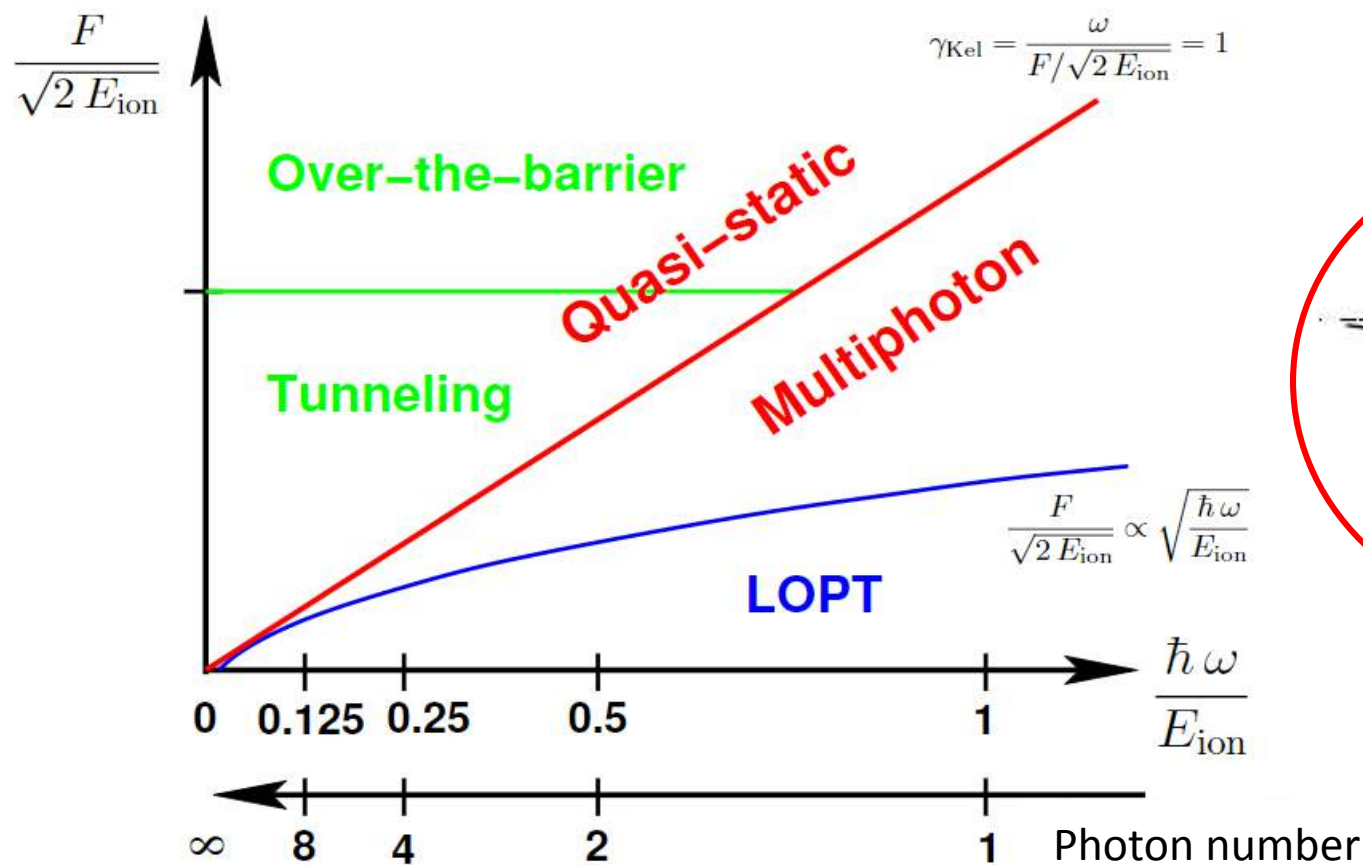
Photoionization regimes



A. Saenz: Atoms and Molecules in
 B. Intense Laser Fields, Berlin 2014

$F \uparrow, \omega \downarrow$ - tunneling

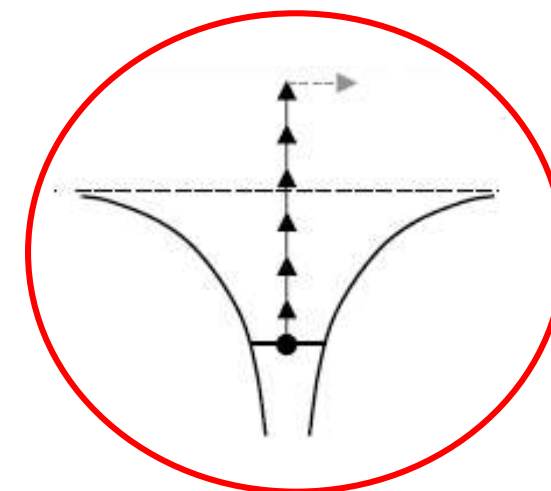
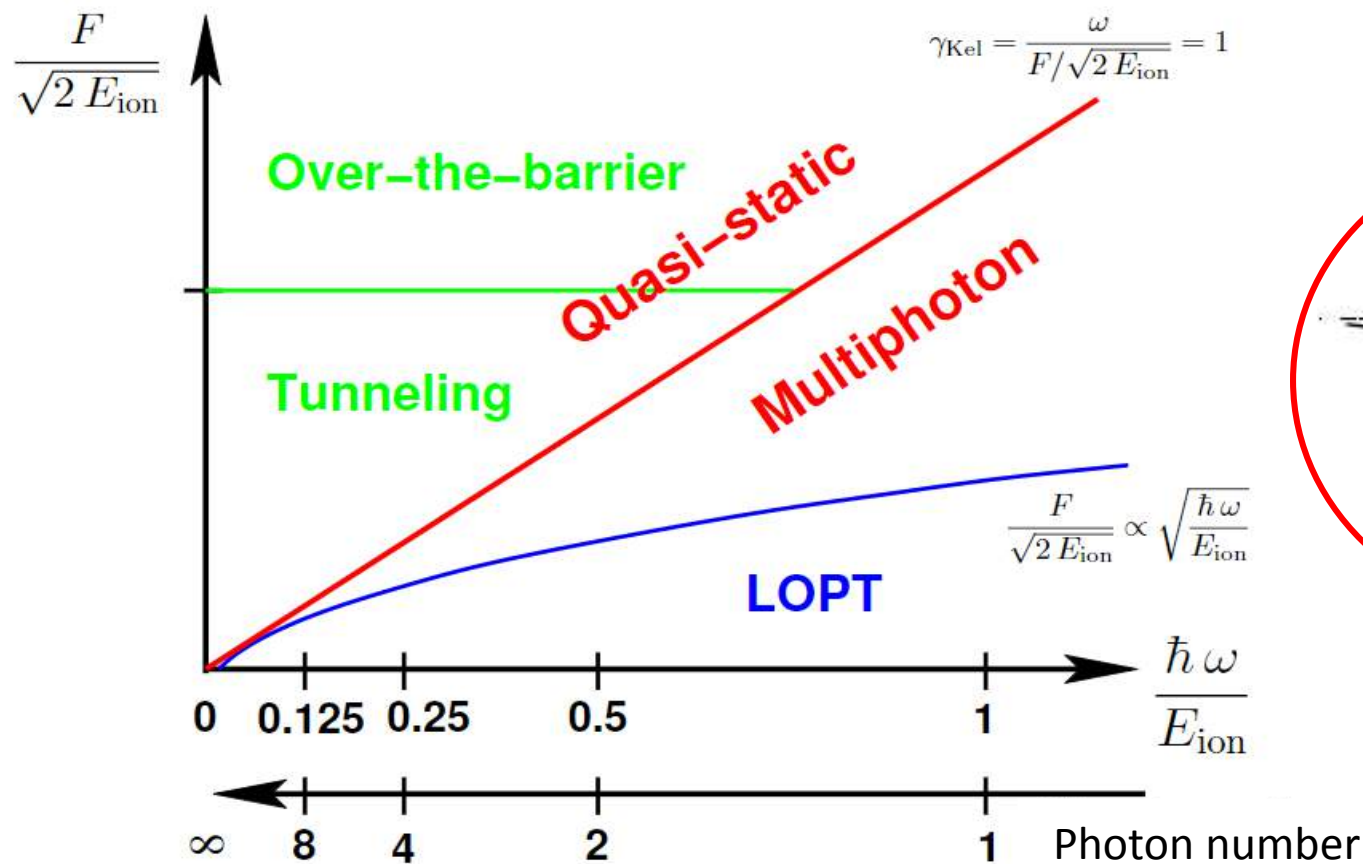
Photoionization regimes



A. Saenz: Atoms and Molecules in
 B. Intense Laser Fields, Berlin 2014

$F \downarrow, \omega \uparrow$ - multiphoton

Photoionization regimes



A. Saenz: Atoms and Molecules in
 B. Intense Laser Fields, Berlin 2014

$$\Gamma_{\text{LOPT}} \propto I^N \left| \sum_{\nu, \mu, \dots, \zeta} \frac{\langle \Psi_f | \hat{D} | \Psi_\nu \rangle \langle \Psi_\nu | \hat{D} | \Psi_\mu \rangle \cdots \langle \Psi_\zeta | \hat{D} | \Psi_i \rangle}{[E_\nu - E_i - (N-1)\omega] [E_\mu - E_i - (N-2)\omega] \cdots [E_\zeta - E_i - \omega]} \right|^2$$

Theoretical assumptions



- $M(i) \longrightarrow M^+(j)$, no inter-channel interaction
- No resonances
- Upon ionization: Coulomb field of the core only
field is neglected;
no $e^- - e^-$ interaction;
- Wave functions: $M(i)$ orthogonal to e^-
- Photoionization threshold law: $E_\omega = I_p + k^2/2$ (one photon)
vs. strong-field regime: peaks at $nE_\omega = I_p + k^2/2$

Dyson orbitals: the concept



Rate of n-photon ionization:

$$\Gamma_n = I^n \sigma$$

Electron
momentum

Photon
energy

$$\sigma_{IF} = 4\pi^2 \underbrace{k}_{\text{Electron momentum}} \underbrace{\omega}_{\text{Photon energy}} |D_{IF}^k|^2,$$

$$D_{IF}^k = \mathbf{u} \langle \underbrace{\phi_{IF}^d}_{\text{Dyson orbital}} | \mathbf{r} | \Psi_{el}^k \rangle$$

From *ab initio*
(Q-CHEM)

$$\underbrace{\phi_{IF}^d(1)(\mathbf{r})}_{\text{Dyson orbital}} = \sqrt{N} \int \underbrace{\Psi_I^N(1, \dots, n)}_{\text{Initial state}} \underbrace{\Psi_F^{N-1}(2, \dots, n)}_{\text{Final state}} d2 \dots dn$$

Free e⁻ w.f. expansion truncated numerically:

$$\Psi_{kf}^{\text{el}}(x, y, z) = \Psi_{kf}^{\text{el}}(r, \theta, \phi) = \sum_{lm} \underbrace{C_{klm}}_{\text{Coefficients}} \underbrace{R_{kl}(r)}_{\text{Coulomb/plane wave}} Y_{lm}(\theta, \phi),$$

Coulomb/plane wave

Implementation: QCHEM + ezDyson



TIME-DEPENDENT INPUT!

QCHEM Input:

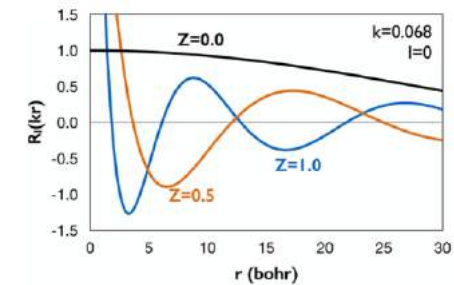
- ✓ Geometry (QMD)
- ✓ method eom-ccsd
- ✓ basis
- ✓ M/M⁺ number of states

QCHEM Output:

- (*Ab initio*)
- ✓ Ionization/excitation energies

EZDYSON Input:

- ✓ Free e parameters (l, Q)
- ✓ Rotational average +/-



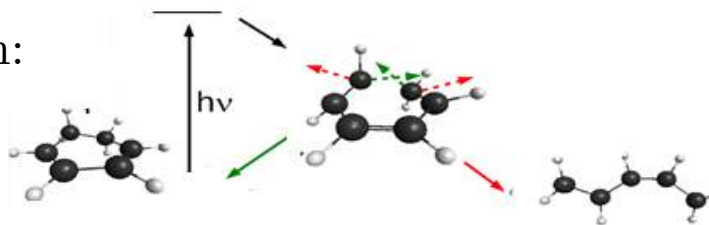
EZDYSON Output:

- ✓ Dyson orbitals (\mathbf{r}) (+plots)
- ✓ Cross section expansion coefficients C_{klm}
- ✓ Cross sections (on the photon energy)
- ✓ Asymmetry parameters

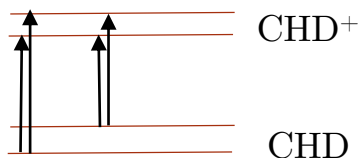
Photoionization of 1,3-Cyclohexadiene (CHD)



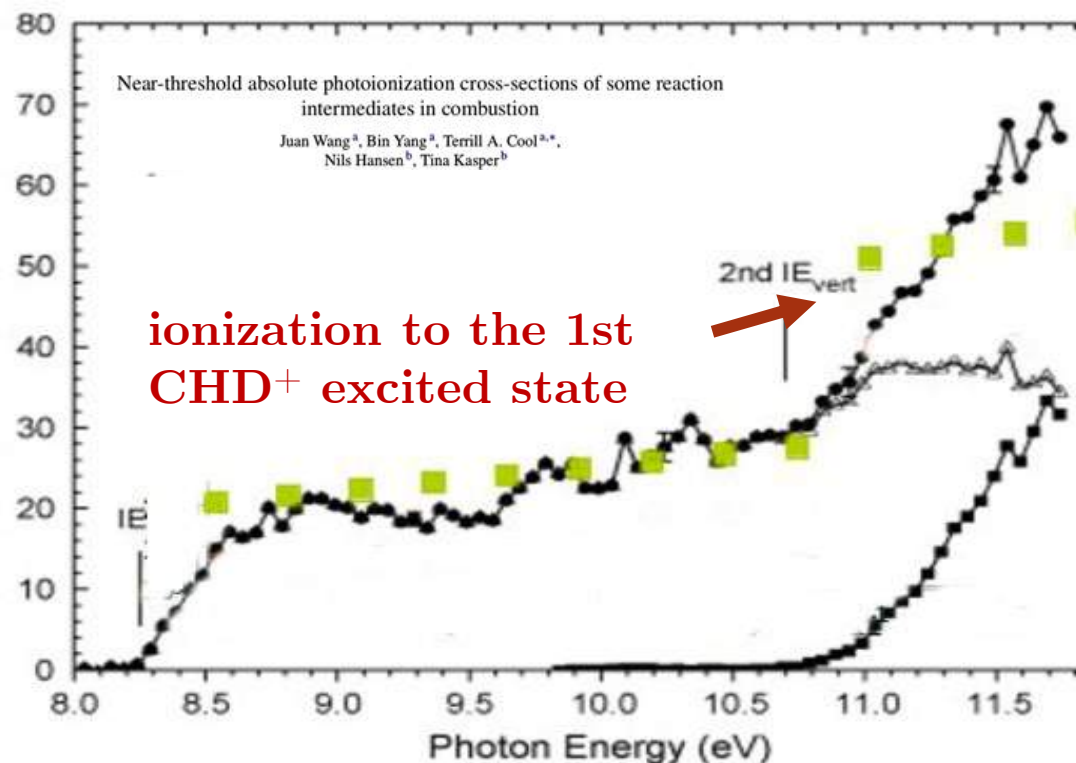
Ring-opening reaction:



Ground-state photoionization



- 4 Dyson orbitals
- Free electron: $l_{\max}=5$
- Orientation-averaged
- Linearly polarized field



CHD: Time-dependent photoionization cross section



QMD:

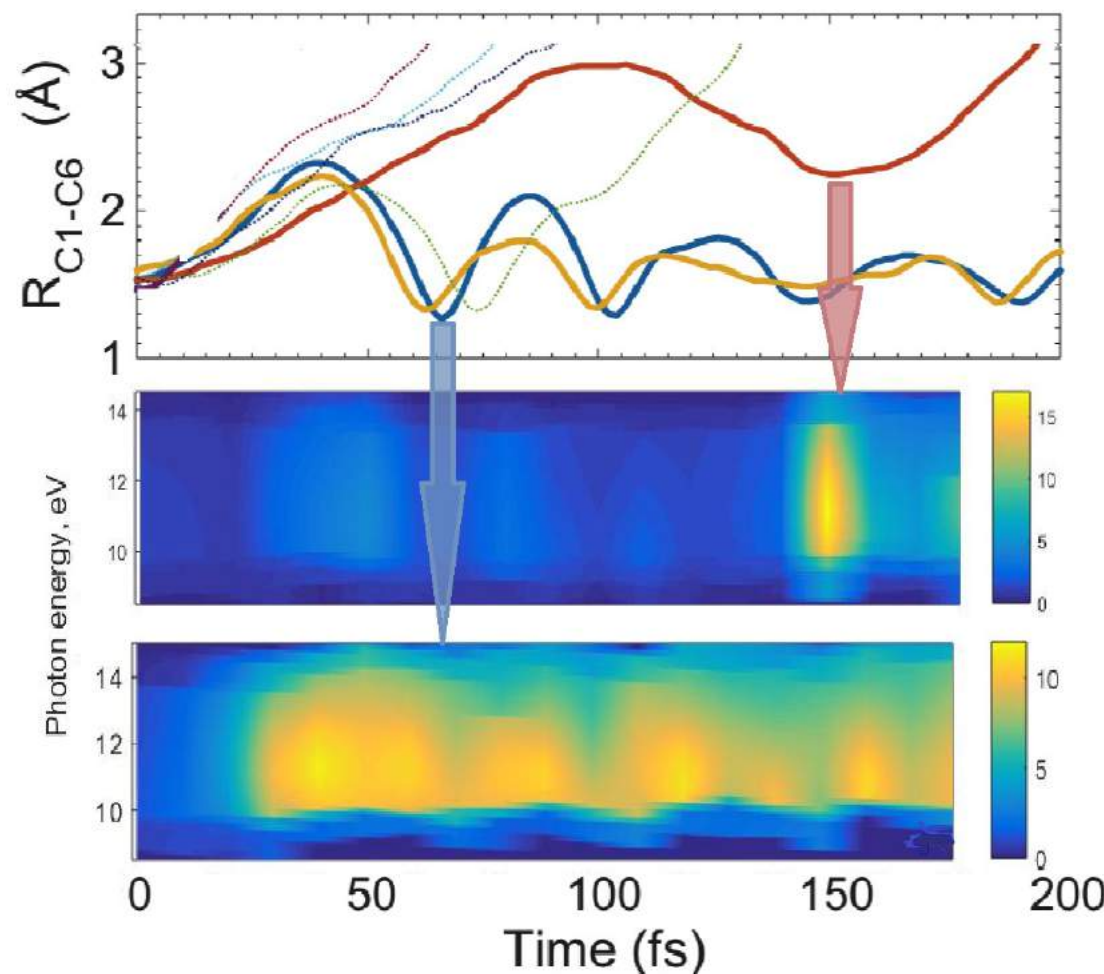
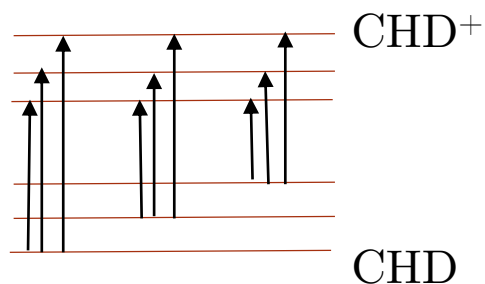
| Trajectory | Weight (%) | Comment |
|------------|------------|------------|
| 16 | 20 | Direct to |
| 1 | 19 | Closed |
| 2 | 18 | Rapid open |
| 65 | 14 | Closed |
| 66 | 10 | Closed |

PRL 114, 255501 (2015) PHYSICAL REVIEW LETTERS 26 JUNE 2015

Imaging Molecular Motion: Femtosecond X-Ray Scattering of an Electrocyclic Chemical Reaction

M. P. Miniti,^{1,2} J. M. Bodarz,^{1,2} A. Kirrander,³ J. S. Robinson,³ D. Ratner,¹ T. J. Lane,^{1,4} D. Zhu,¹ J. M. Glowina,¹ M. Kozina,¹ H. T. Lemke,¹ M. Sikorski,¹ Y. Feng,¹ S. Nelson,¹ K. Saita,¹ B. Stankus,² T. Northey,¹ J. B. Hastings,^{1,2} and P. M. Weber^{2,5}

9 Dyson orbitals



Intensity oscillations reflect the geometry changes!

CS₂: dynamics upon excitation

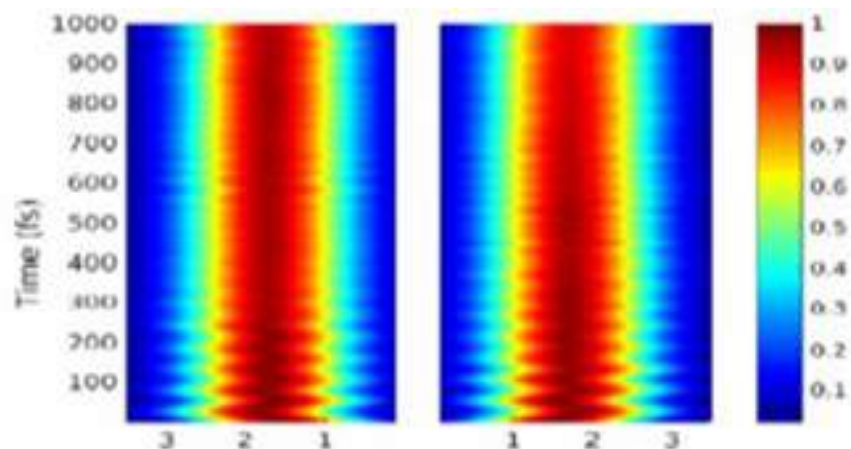


(Credit: Darren Bellshaw)

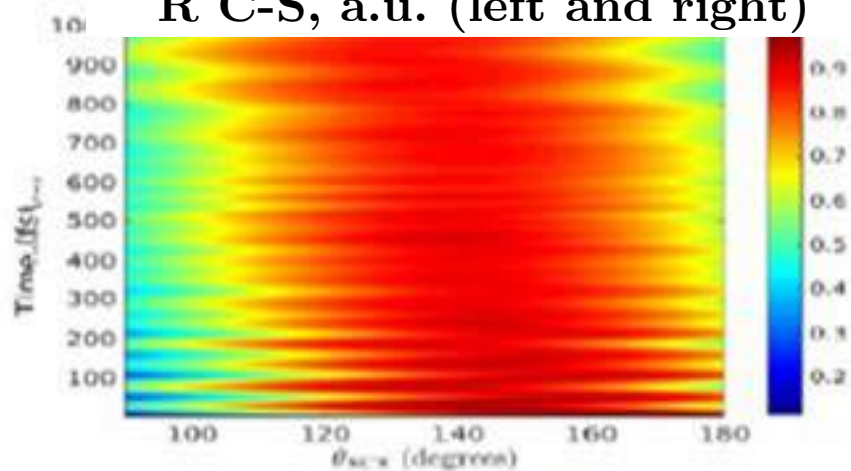
100 classical trajectories

"average trajectory" concept

Total population distribution



R C-S, a.u. (left and right)



The bond angle, degree

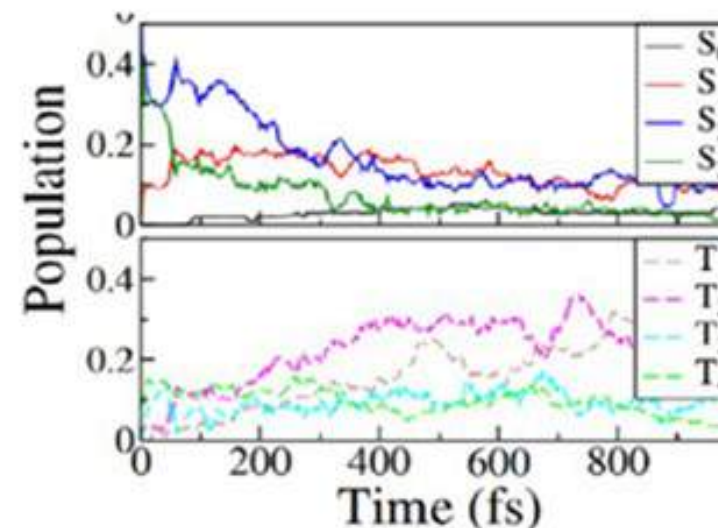
t=100 fs



t=200 fs



t=300 fs

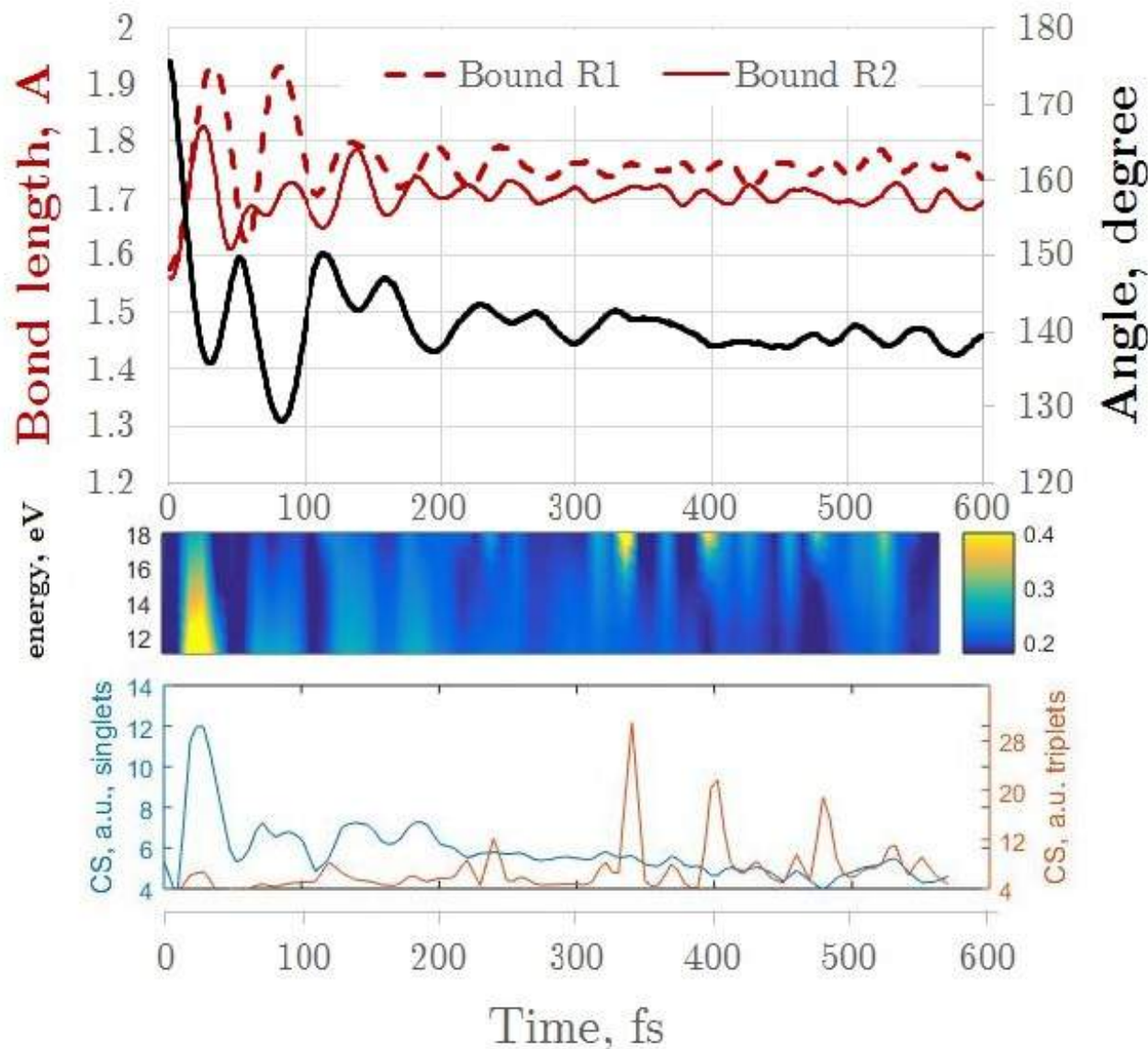


- 8 CS₂ states are involved (4 singlets, 4 triplets)
- N ionic states can be included => N*8 transitions
- Total S ↓, total T ↑

CS₂: time-dependent photoionization



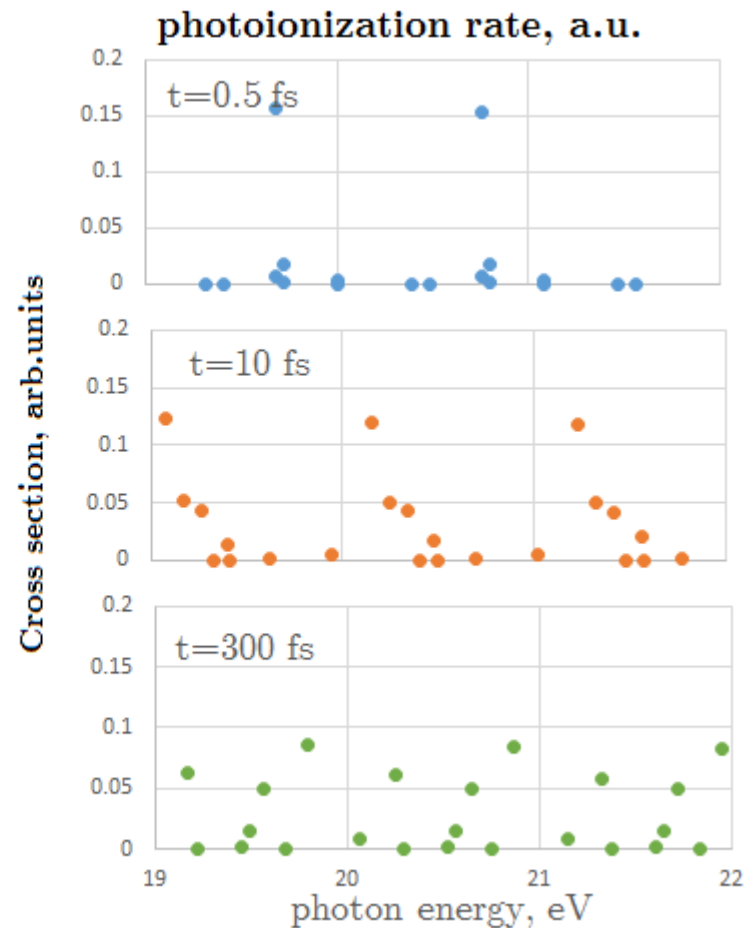
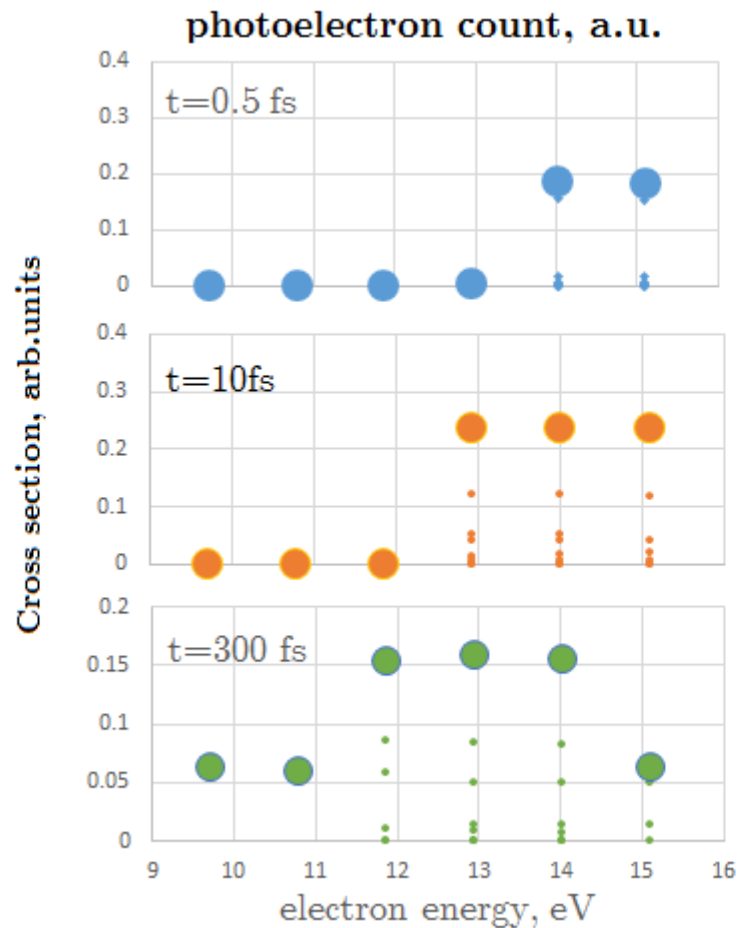
Geometry oscillations along the “average” trajectory:



CS₂: channel-resolved photoelectron spectrum



$$E_{\omega} = I_p + k^2/2$$



CS₂: free e⁻ angular momentum distribution



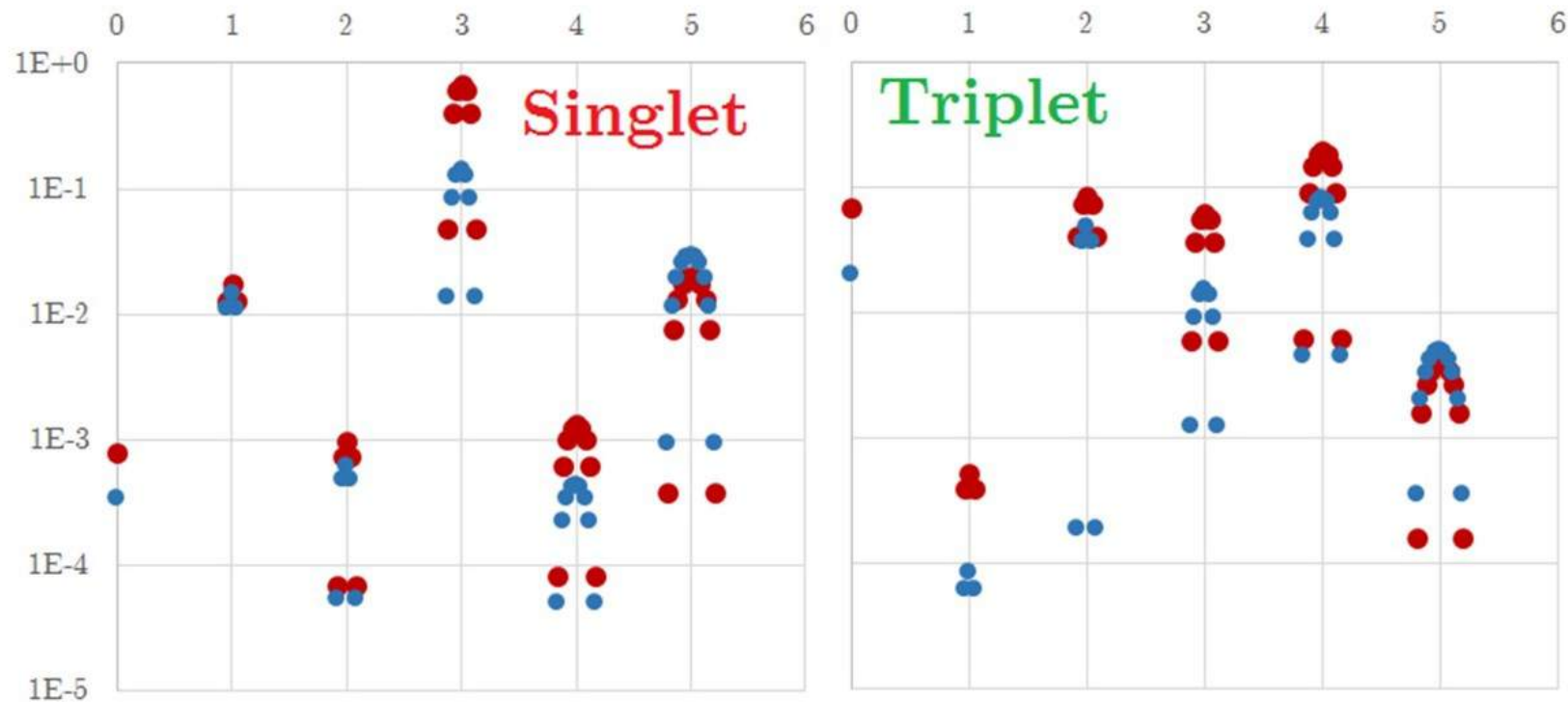
(C_{klm})

1 fs

l=(0...5)

330 fs

l=(0...5)



— E_k=6.6eV

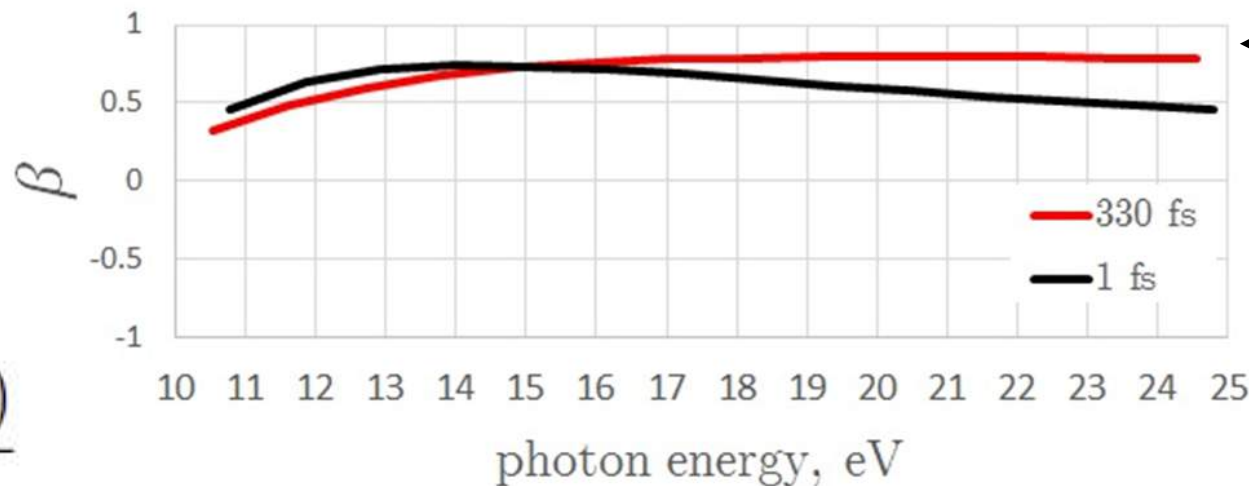
— E_k=13.6eV

CS₂: anisotropy parameter



$$\beta = \frac{2(\sigma_{par} - \sigma_{perp})}{\sigma_{par} + 2\sigma_{perp}}$$

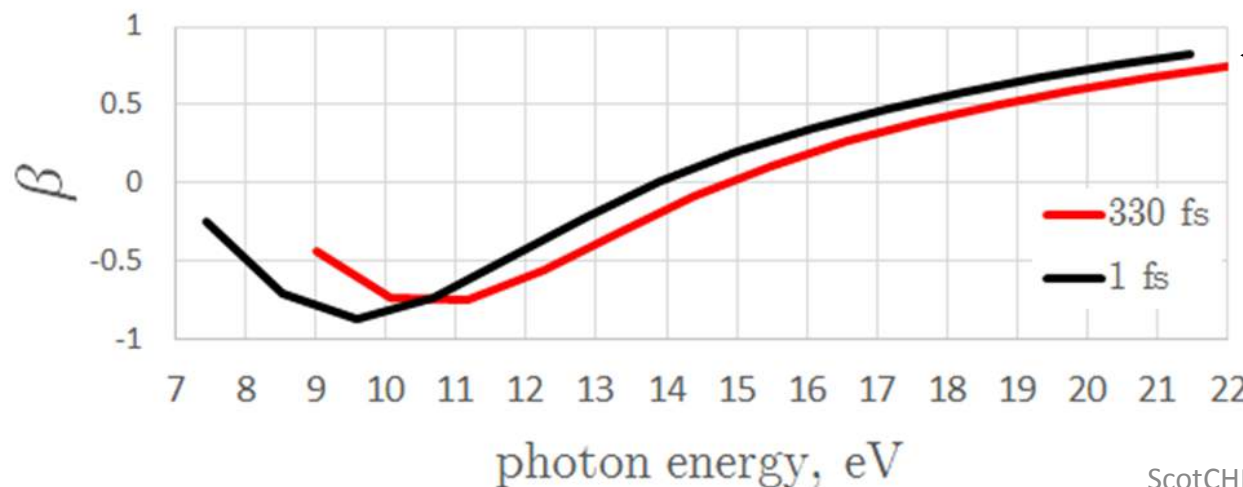
Singlet



----- Anisotropic

----- No parallel ionization

Triplet



----- Anisotropic

----- No parallel ionization

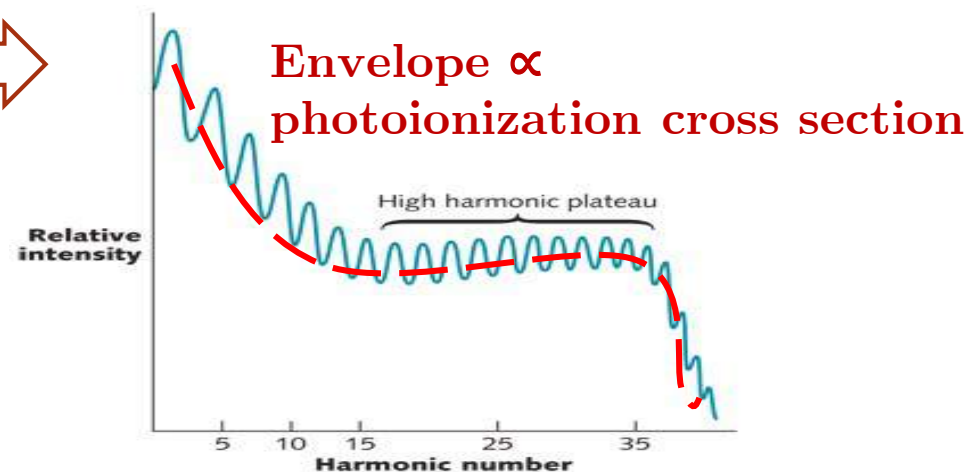
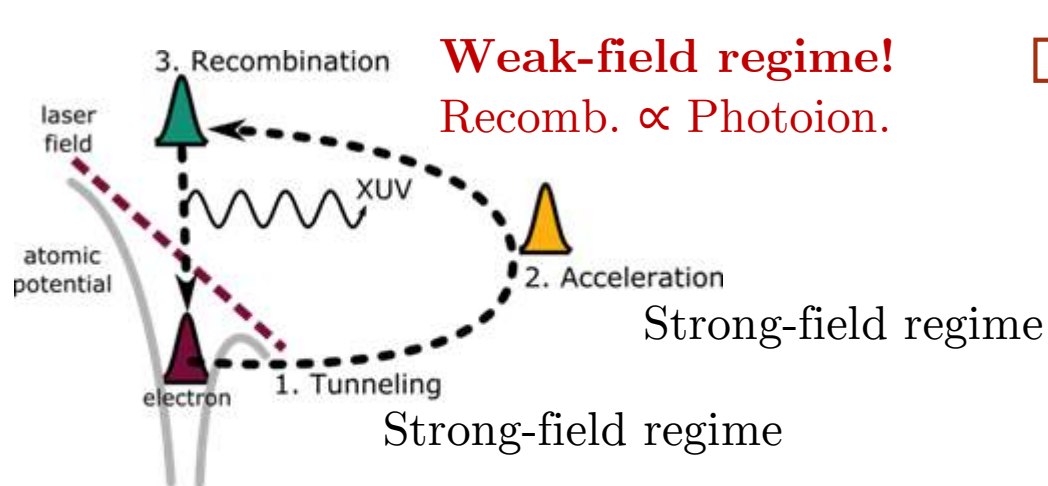
Conclusions + Next steps:



Photoionization:

- ✓ Tool to analyse pump-probe experiments
- ✓ Photoionization signal reflects structural changes!
- CS₂: photoelectron spectra vs. experiment
- CHD: full ring opening reaction of 1,3-cyclohexadiene

High-harmonic generation (HHG)





Acknowledgements

- Edinburgh: Adam Kirrander, Darren Bellshaw
- Southampton: Russell Minns (experimental group)
- Hokkaido, Japan: Kenichiro Saita
- ezDyson team: Samer Gozem

&

Thank you!









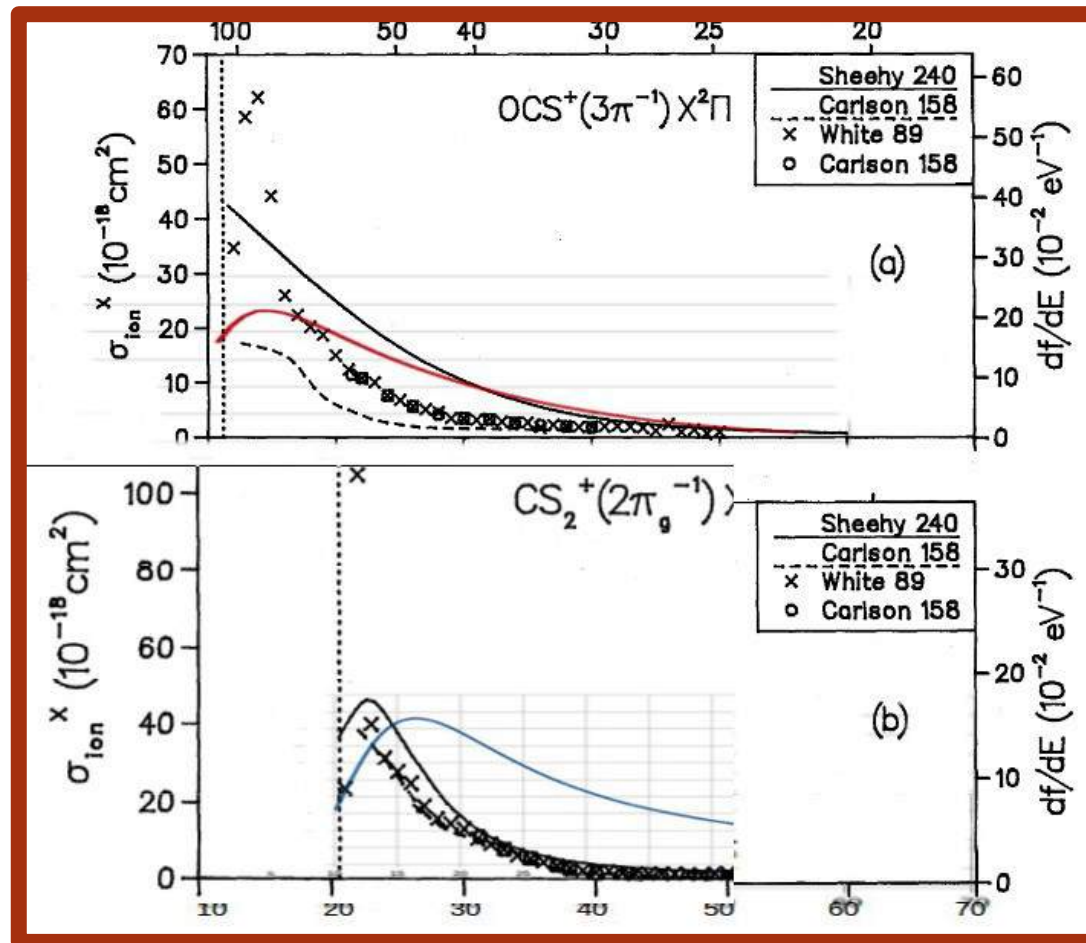


CS₂: photoionization from the ground state



- Cooper minimum – due to the shape of the orbital and the continuum state;
- Should be visible in the HHG spectrum

CS₂ vs. OCS



J.J. Yeh and I. Lindau.
At. Data Nucl. Data Tables 1985, 21, 1.


Next steps: Photoionization and HHG



- Saddle-point approximation:

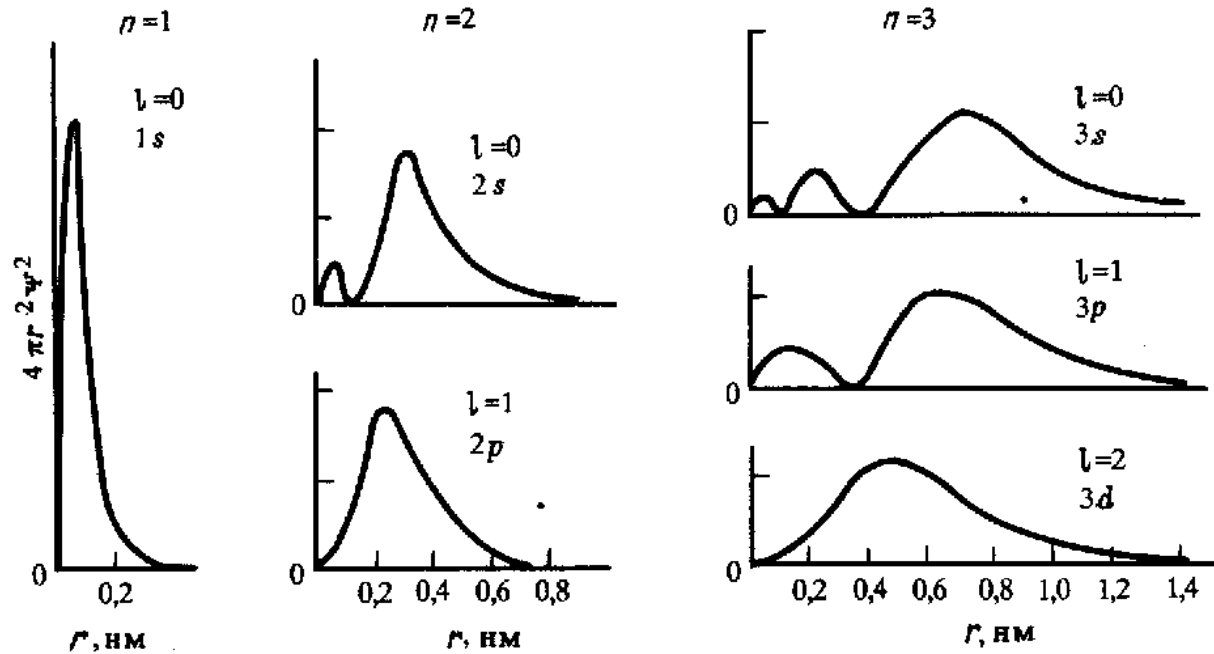
High-Harmonic Generation: **Ionization** + Free electron acceleration + **Electron Photorecombination**
 $I_p(R(t))$ $F(t)$ $I_p(R(t))$; Energy $(R(t))$

Quantitative Rescattering Theory (Le et. al):

$$S^{QRS}(\omega, \theta) = \frac{N(\theta)}{N^{ref}} \frac{\sigma(\omega, \theta)}{\sigma^{ref}(\omega)} S^{ref}(\omega)$$


- Photorecombination at the low field intensity: multiphoton regime  DO approach!

Radial part of atomic orbitals



Occurrence of Cooper minimum
In atoms

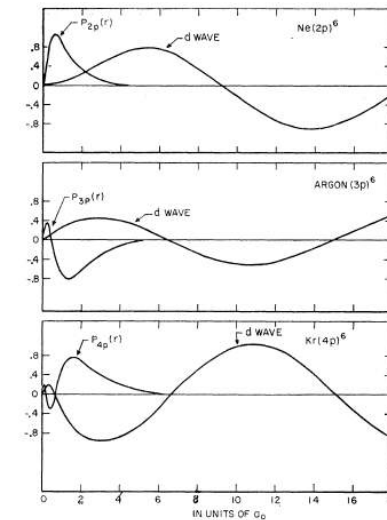


FIG. 2. Outer subshell radial wave functions and d waves for $l=0$ for Ne, Ar, and Kr.